

# DFT+DMFT for Oxide Heterostructures

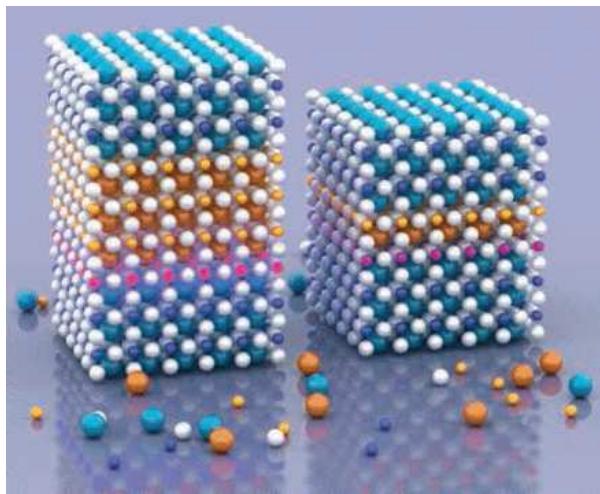
Frank Lechermann

*Theoretische Physik III, Ruhr-Universität Bochum, Germany*

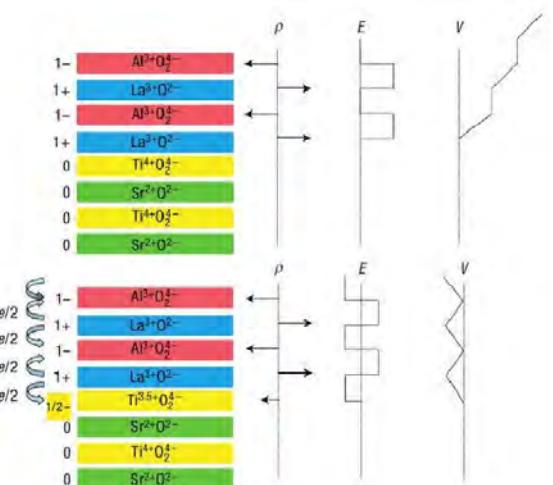
**Autumn School on Correlated Electrons:  
Dynamical Mean-Field Theory of Correlated Electrons  
4-7 October 2022, Forschungszentrum Jülich**

# Oxide Heterostructures : (selected) Phenomenology

- superlattice/thin film build from
  - SrTiO<sub>3</sub> (band insulator)
  - LaAlO<sub>3</sub> (band insulator)
  - LaTiO<sub>3</sub> (Mott insulator)
  - ⋮
- possible quasi-twodimensional electron system (2DES)
- instabilities : ferromagnetism, superconductivity, . . .



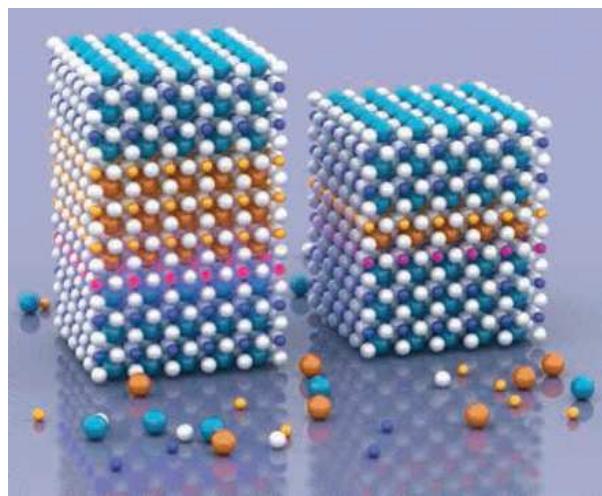
e.g. [Hwang et al., Nature Mat. 11, 103 (2012)]



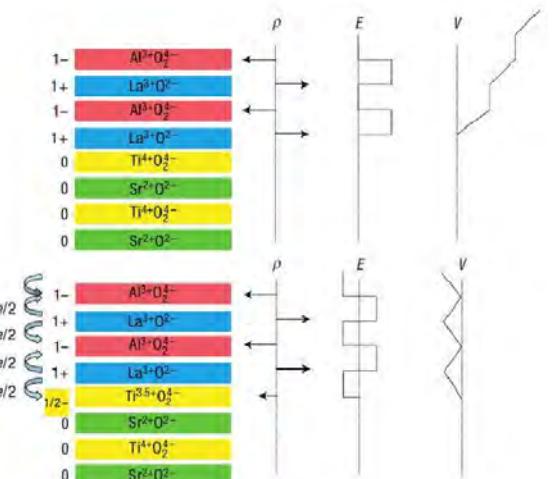
[Nakagawa et al., Nature Mat. 5, 204 (2006)]

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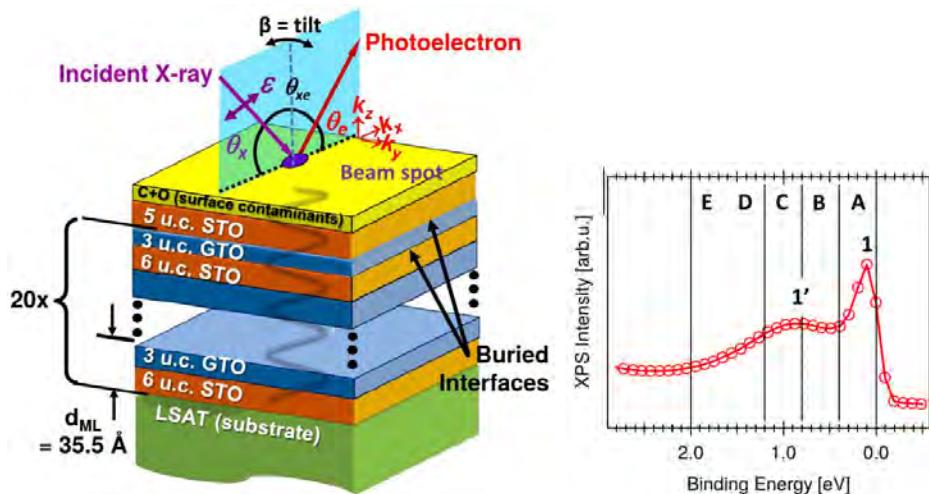


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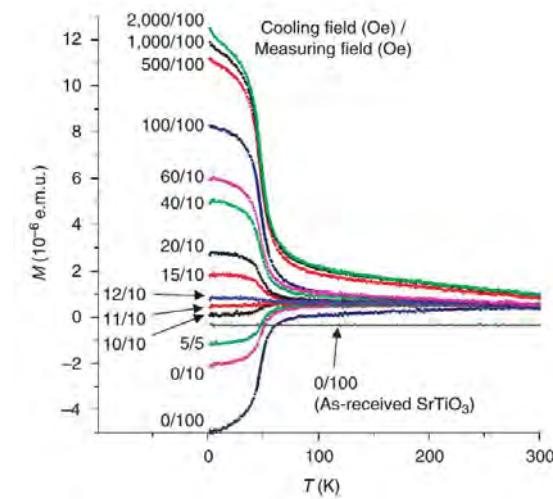
[Nakagawa et al., Nature Mat. 5, 204 (2006)]

band-Mott insulators e.g. SrO/GdTiO<sub>3</sub>



[Nemšák et al., PRB 93, 245103 (2016)]

band-band insulators e.g. LaAlO<sub>3</sub>/SrTiO<sub>3</sub>



[Ariando et al., Nat. Commun. 2, 188 (2015)]

# Oxide Heterostructures : Theoretical Work

- model-Hamiltonian dynamical mean-field theory (DMFT) for Mott/band-insulator interfaces

[Okamoto and Millis, *Nature* 428, 630 (2004)]

- density functional theory (DFT) for band-insulating heterostructures

[Popovic and Satpathy, *PRL* 94, 176805 (2005)]

- DFT plus static Hubbard correlations (DFT+U) for band- and Mott heterostructures

[Pentcheva and Pickett, *PRL* 99, 016802 (2007)] [Pavlenko et al., *PRB* 86, 064431 (2012)]

- model-Hamiltonian field-theoretical approach to  $\text{LaAlO}_3/\text{SrTiO}_3$

[Joshua et al., *Nat. Commun.* 3, 1129 (2012)]

- (realistic) Anderson-Hamiltonian exact-diagonalization/Lanczos method for isolated-defect  $\text{SrTiO}_3$

[Lin and Demkov, *PRL* 111, 217601 (2014)]

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## this talk

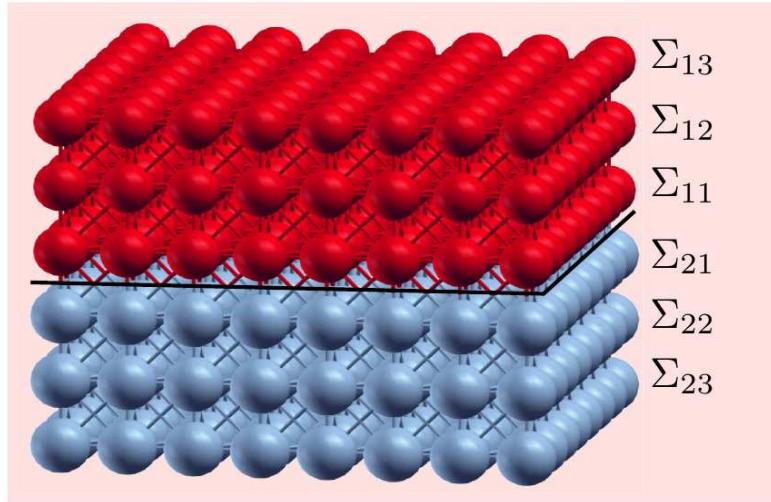
★ realistic many-body approach via DFT+DMFT

★ correlation physics by design

★ other recent DFT+DMFT approaches to oxide heterostructures

[K. Held, G. Sangiovanni, P. Hansmann, J. Tomczak] [C. Ederer] [C. Marianetti, A. J. Millis], [E. Dagotto], ...

# Oxide Heterostructures : Why at all?



## issues and features

- charge transfers and electrostatic boundary conditions
- spin and orbital reconstructions
- compressive and tensile strain
- source/sink for additional (point) defects
- two-dimensional characteristics

## prospects

- unique, well-defined doping scenario
- tuning (proximity) options building up on the bulk
- (control of) layer-selective physics
- possibly novel (emergent) electronic phases
- oxide membranes and merging oxides with other materials

# Outline

- theory: from DFT to DFT+DMFT
- interfacing band insulator with band insulator
- interfacing band insulator with Mott insulator
- natural-heterostructure systems: delafossites

# Density Functional Theory (DFT) : Effective Single-Particle Approach

electronic density functional theory (DFT) with approximate exchange-correlation

- DFT is ground-state many-body theory with inhomogeneous charge density  $n(\mathbf{r})$  ( $\Leftrightarrow \Psi(\{\mathbf{r}_i \sigma_i\})$ ) as central quantity, formally exact

$$E[n] = T[n] + \int d\mathbf{r} n(\mathbf{r}) v_{\text{ext}}(\mathbf{r}) + E_{\text{H}}[n] + \mathbf{E}_{\text{xc}}[\mathbf{n}]$$

- approximate exchange-correlation functional  $\mathbf{E}_{\text{xc}}$  in effective single-particle Kohn-Sham mapping to render the approach practicable

local density approximation (LDA) : homogeneous electron gas is reference  
generalized-gradient approximation (GGA) :  $\nabla n$  corrections to LDA



W. Kohn, Nobel Prize 1998

- works very well for many realistic systems !  
→ many molecules, simple metals, semiconductors (not band gap), . . .

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- PROBLEM: insufficient for materials with strong correlations among the electrons !

- ✗ some systems with odd electron number in unit cell are isolating
- ✗ satellite structures in one-particle spectral function
- ✗ strong changes of spectral function with doping
- ✗ metal-to-insulator transition without symmetry change
- ✗ coherence temperatures and generally subtle behavior with temperature
- ⋮

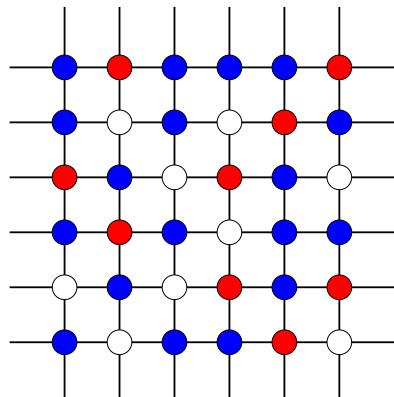
# Correlated Electrons : Quasiparticles and Coherence, intuitively



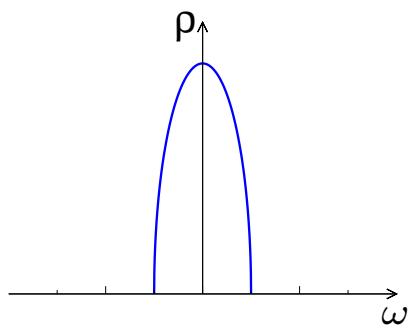
# Correlated Electrons : Mott-Hubbard picture

Hubbard model:  $H = -\mathbf{t} \sum_{\langle ij \rangle \sigma} c_{i\sigma}^\dagger c_{j\sigma} + \mathbf{U} \sum_i n_{i\uparrow} n_{i\downarrow}$ , for half filling  $n = 1$

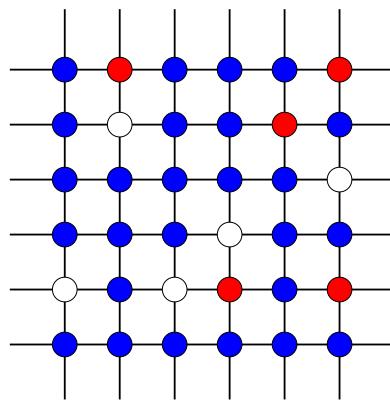
nonint. limit ( $U = 0$ )



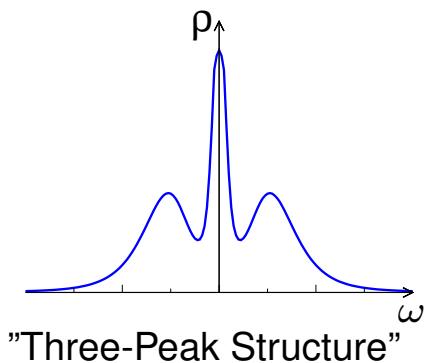
- $H = \sum_{\mathbf{k}\sigma} \varepsilon_{\mathbf{k}} c_{\mathbf{k}\sigma}^\dagger c_{\mathbf{k}\sigma}$
- ideal metal, Fermi gas



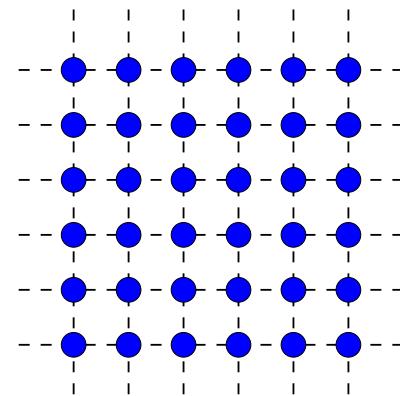
intermediate ( $U \sim t$ )



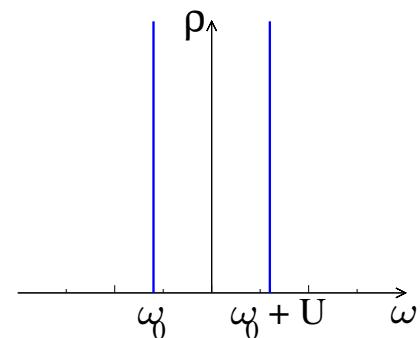
- correlated metal
- dominance of single occupations



atomic limit ( $t = 0$ )

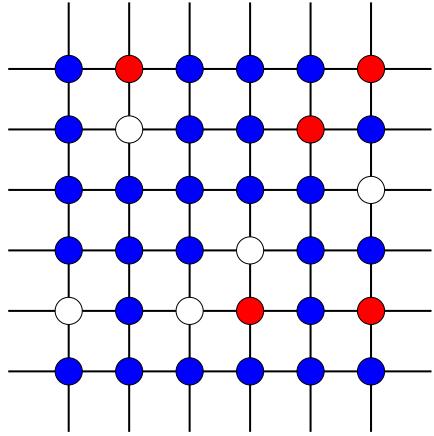


- decoupled lattice sites
- only single occupations in ground state

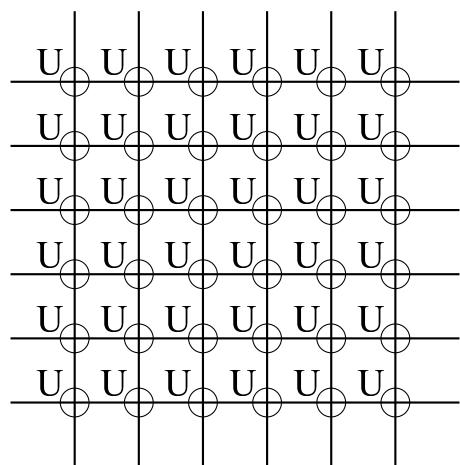


# Dynamical Mean-Field Theory (DMFT) : Many-Body Approach

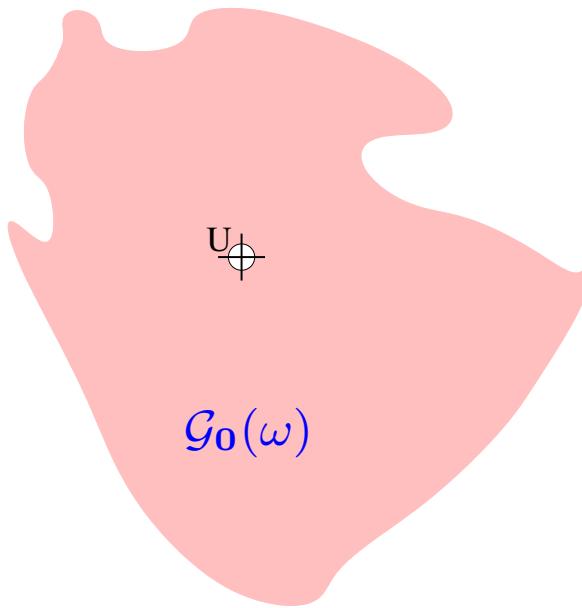
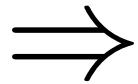
[Metzner, Vollhardt, PRL (1989)] [Georges, Kotliar, PRB (1992)]



$$H = -t \sum_{\langle ij \rangle \sigma} c_{i\sigma}^\dagger c_{j\sigma} + U \sum_i n_{i\uparrow} n_{i\downarrow}$$



$$G_{\text{loc}}(\omega) = \sum_{\mathbf{k}} [\omega + \mu - \varepsilon_{\mathbf{k}} - \Sigma(\mathbf{k}, \omega)]^{-1}$$



$$G_{\text{imp}}(\omega) = [\mathcal{G}_0^{-1}(\omega) - \Sigma_{\text{imp}}(\omega)]^{-1}$$

**DMFT approximation:**

$$G_{\text{loc}}(\omega) \stackrel{!}{=} G_{\text{imp}}(\omega)$$

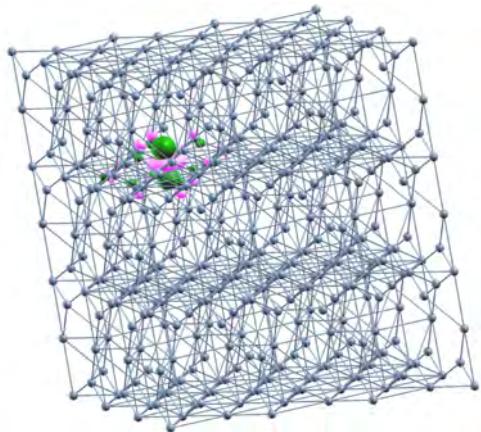
$$G_{\text{loc}}^{\text{DMFT}}(\omega) = \sum_{\mathbf{k}} [\omega + \mu - \varepsilon_{\mathbf{k}} - \Sigma_{\text{imp}}(\omega)]^{-1}$$

→ local correlations are fully taken into account non-perturbatively, explicit non-local correlations are neglected

# Correlated Materials : different levels of correlation

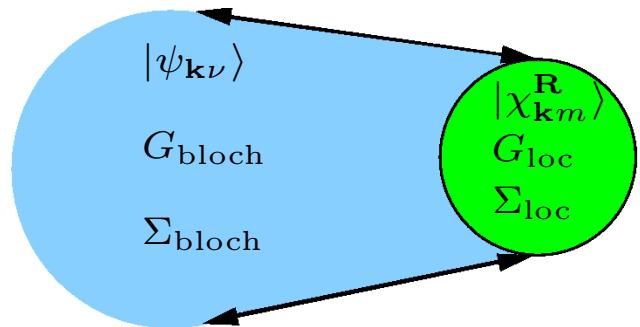
## density functional theory (DFT)

- Hohenberg-Kohn theorems, Kohn-Sham construction, exchange-correlation functional, . . .
- mapping interacting electrons onto non-interacting electrons in an complicated effective potential
- very good description of the realistic, single-particle based chemical bonding ( $\rightarrow$  band structure for solids)

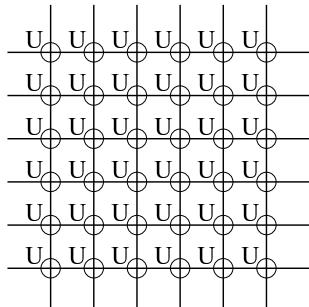


### interface

- define correlated subspace by Wannier(-like) orbitals from correlated sites



## dynamical mean-field theory (DMFT)

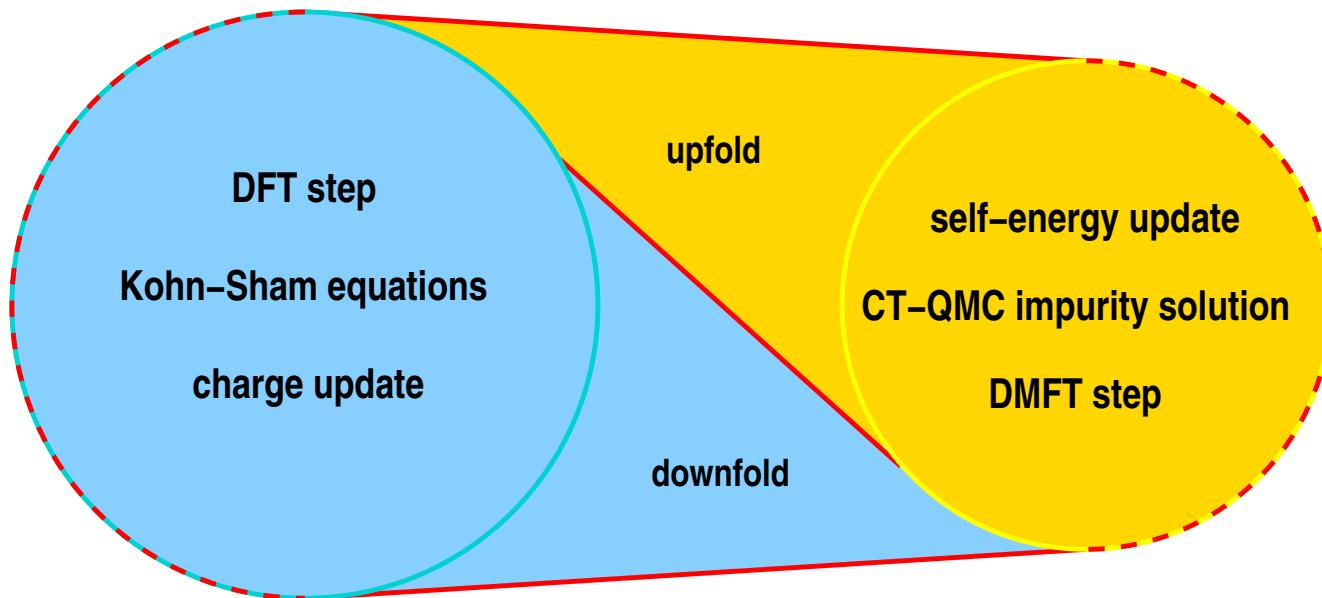


- many-body Green's functions, Hubbard model, quasiparticles vs. Hubbard bands, finite temperature, . . .
- mapping interacting electrons onto an interacting impurity in a self-consistent bath
- very good description of modelized interacting electrons on a lattice

# Realistic Many-Body

[Anisimov, Poteryaev, Korotin et al., JPCM 9, 7359 (1997)] [Lichtenstein and Katsnelson, PRB 57, 6884 (1998)]  
[Held, Keller, Eyert et al., PRL 86, 5345 (2001)] [Pavarini, Biermann, Poteryaev et al., PRL 92, 176403 (2004)]  
[Minár, Chioncel, Perlov, at al., PRB 72, 045125 (2005)] [Kotliar, S. Y. Savrasov, K. Haule et al, RMP 78, 865 (2006)]  
[FL, Georges, Poteryaev et al., PRB 74, 125120 (2006)] [Grieger, Piefke, Peil and FL, PRB 86, 155121 (2012)] ..., ..., ...

## Density Functional Theory (DFT) + Dynamical Mean-Field Theory (DMFT)



- DFT part : mixed-basis pseudopotential

[Meyer, Elsässer, Lechermann and Fähnle, MPI for Metals Research]

- DMFT impurity solver : hyb-CT-QMC (TRIQS code)

[Parcollet et al., Comput. Phys. Commun. 196, 398 (2015)]

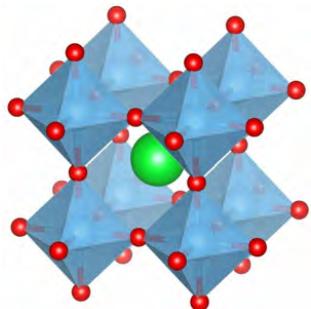
[Seth et al, Comput. Phys. Commun. 200, 274 (2016)]

- charge self-consistency

- 1-5 local correlated orbitals



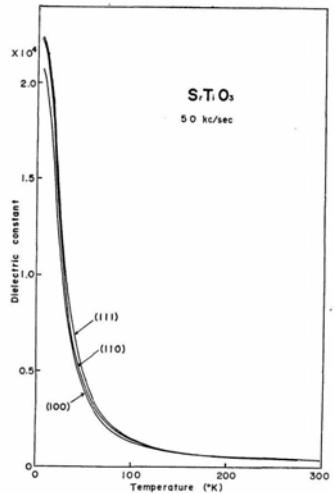
# Bulk SrTiO<sub>3</sub> : A Band Insulator prone to a Plethora of Physics



- cubic perovskite, transition to tetragonal phase at low temperature
- band insulator ( $\Delta_g \sim 3.2$  eV)

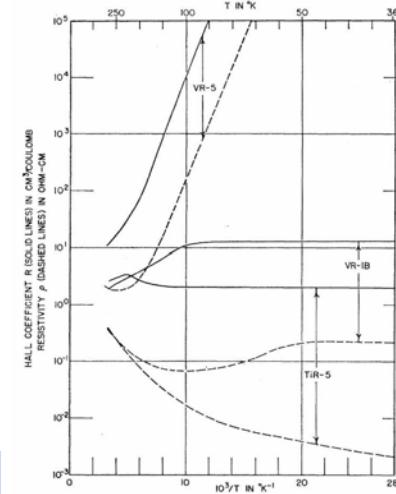
paraelectric

[Sawaguchi et al., JPSN 17, 1666 (1962)]



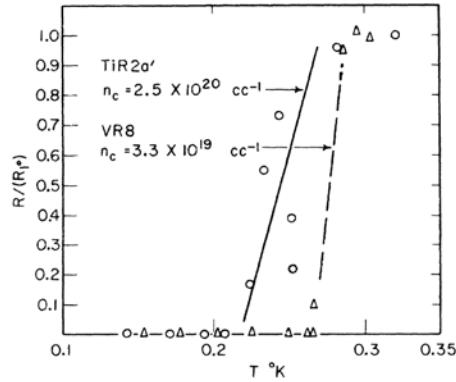
semiconductor

[Frederikse et al., PR 134, A442 (1964)]



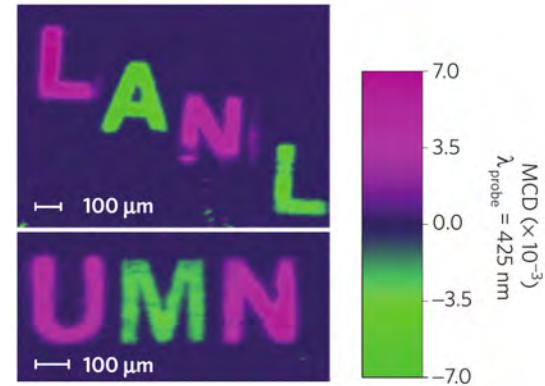
superconductor

[Schooley et al., PRL 12, 474 (1964)]



magnet

[Rice et al. Nat. Mater. 13, 481 (2014)]



# Emergent Physics at the LaAlO<sub>3</sub>/SrTiO<sub>3</sub> Interface

LETTERS

PUBLISHED ONLINE: 4 SEPTEMBER 2011 | DOI: 10.1038/NPHYS2080

nature  
physics

## Coexistence of magnetic order and two-dimensional superconductivity at LaAlO<sub>3</sub>/SrTiO<sub>3</sub> interfaces

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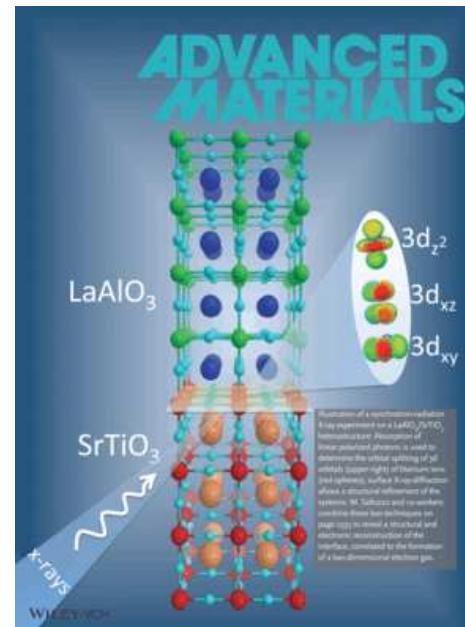
nature  
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PUBLISHED ONLINE: 2 JUNE 2013 | DOI: 10.1038/NMAT3674

## Titanium $d_{xy}$ ferromagnetism at the LaAlO<sub>3</sub>/SrTiO<sub>3</sub> interface

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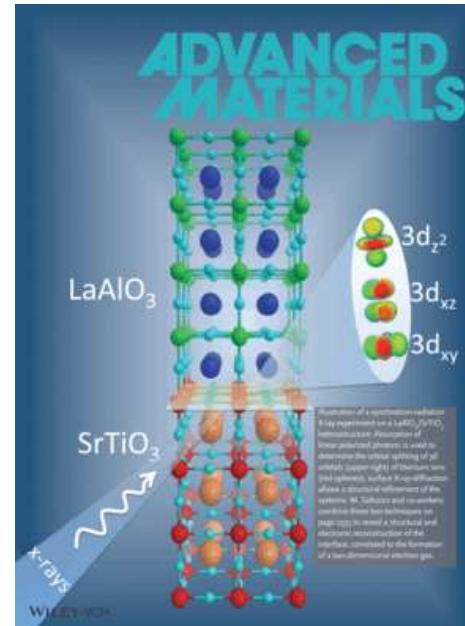
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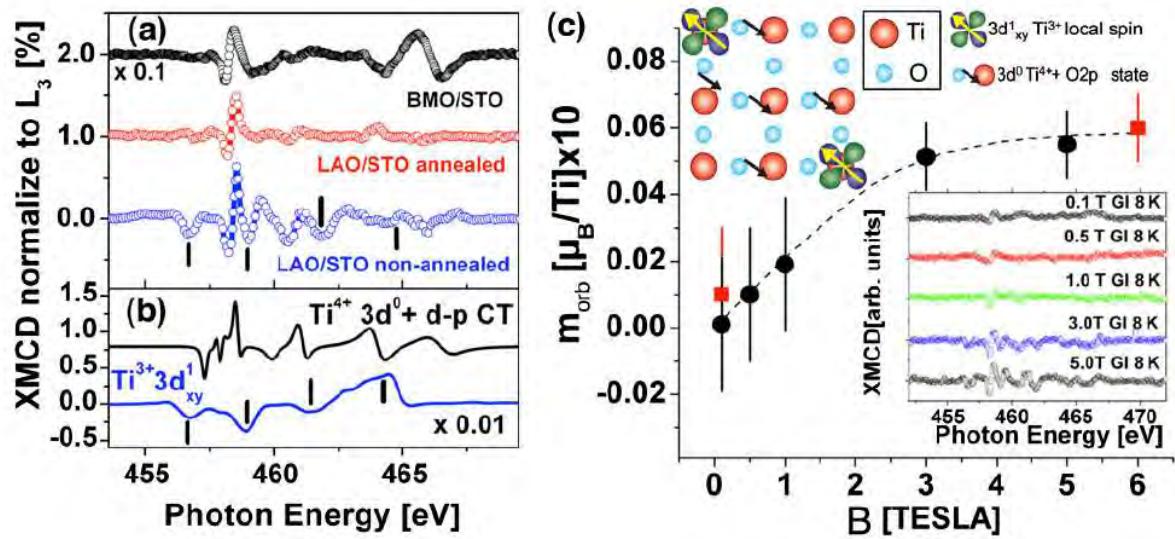
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## RIXS and XMCD measurements relevance of oxygen vacancies at the interface

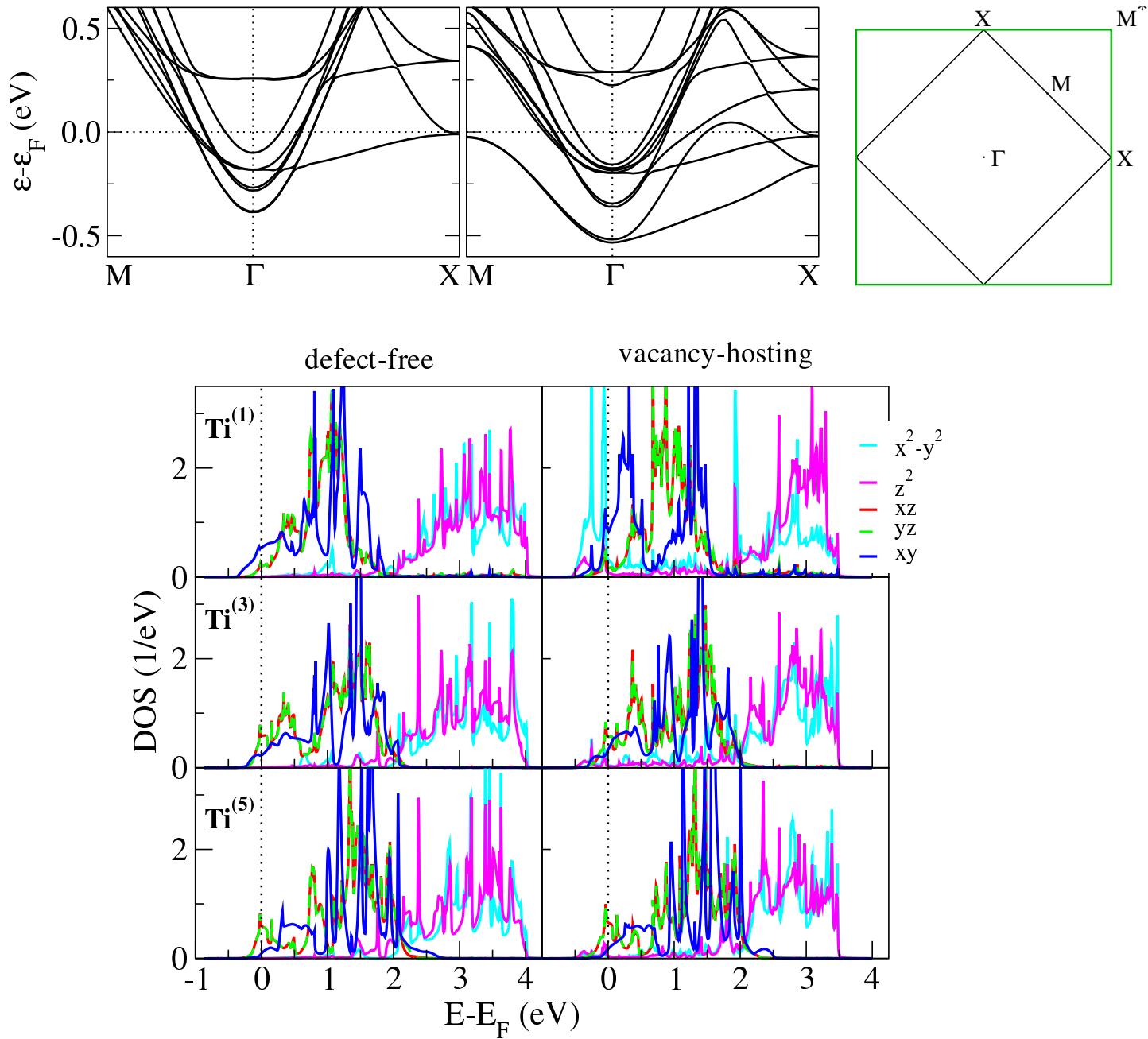
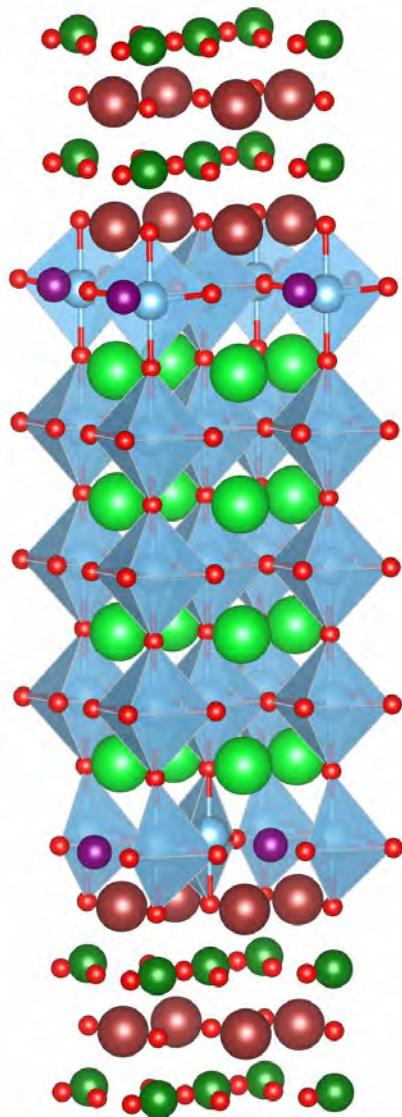
[Park et al., PRL 110, 017401 (2013)]

[Salluzzo et al., PRL 111, 087204 (2013)]



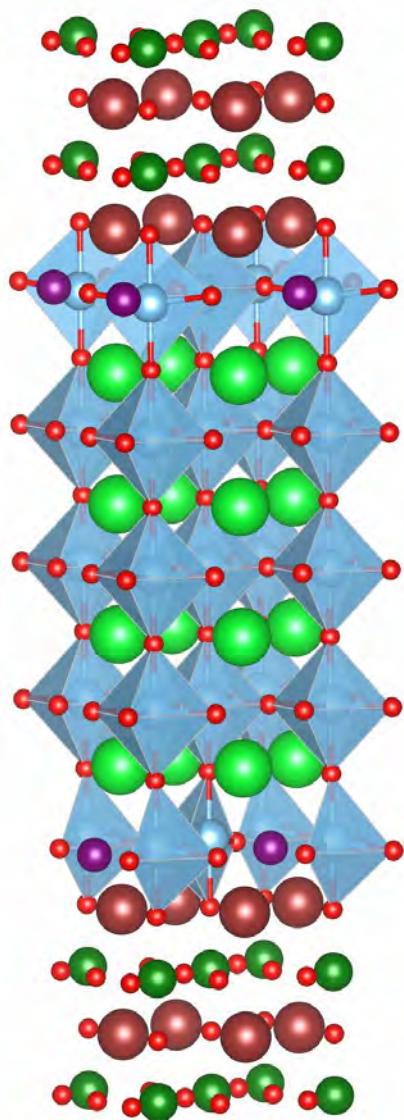
oxygen vacancies introduce electrons that localize at the nearby Ti sites ( $m \sim 0.1 - 0.2\mu_B$ )

# LaAlO<sub>3</sub>/SrTiO<sub>3</sub> interface: DFT results

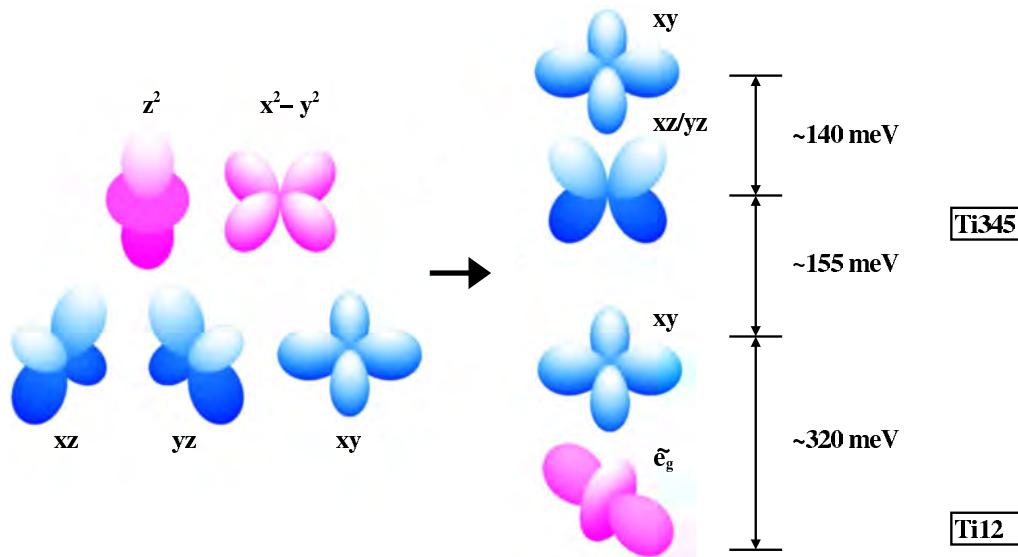
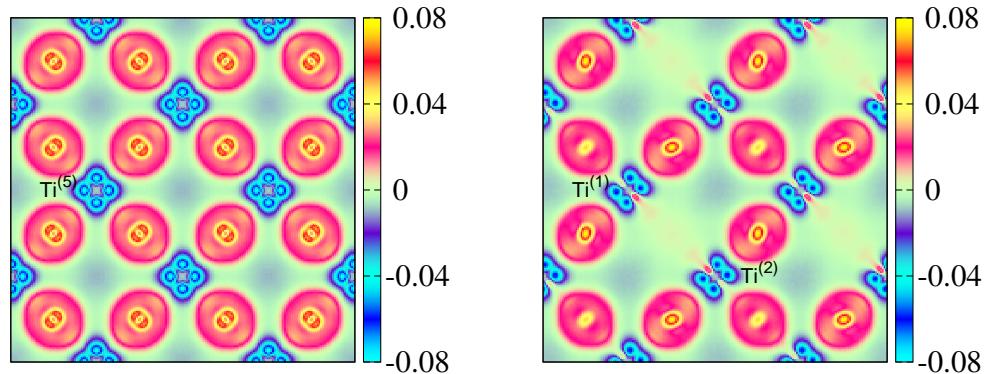


see also [Pavlenko et al., PRB 85, 020407(R) (2012); PRB 88, 201104(R) (2013)]

# LAO/STO dense-defect interface : Relevant States



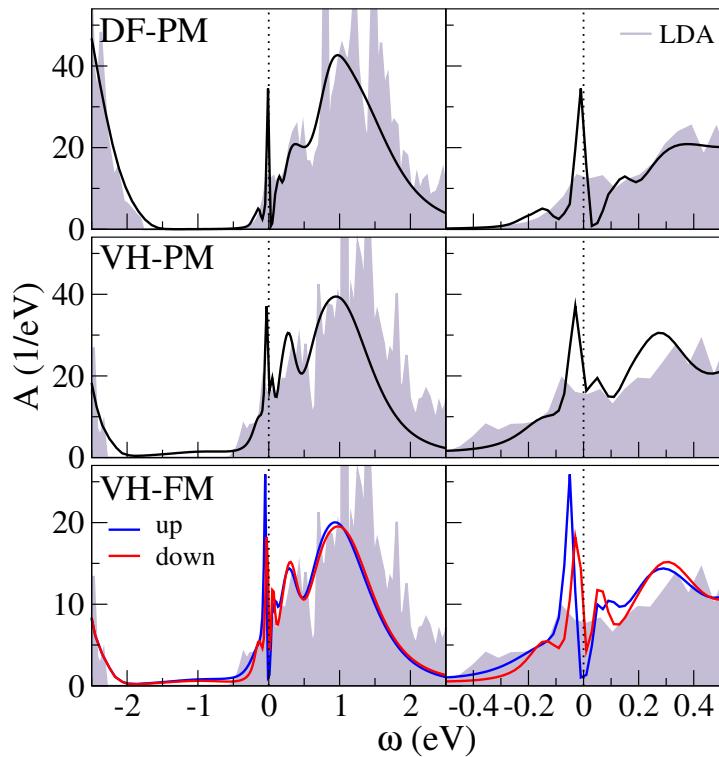
in-plane bond  
charge density  
 $\rho - \rho_{\text{at}}$



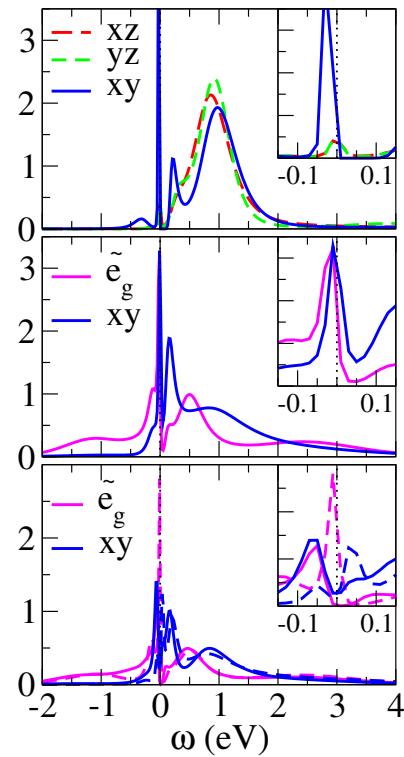
- two-orbital correlated subspace for each Ti ion from orbital projection
- interface Ti:  $\tilde{e}_g - t_{2g}(xy)$  description, with  $|\tilde{e}_g\rangle \sim 0.55|z^2\rangle \pm 0.84|x^2-y^2\rangle$   
 $\Rightarrow$  **coexisting localized and itinerant electrons expected !**
- $\rightarrow$  in line with RIXS measurements [Zhou et al., PRB 83, 201402(R) (2011)]

# LAO/STO dense-defect interface : DFT+DMFT

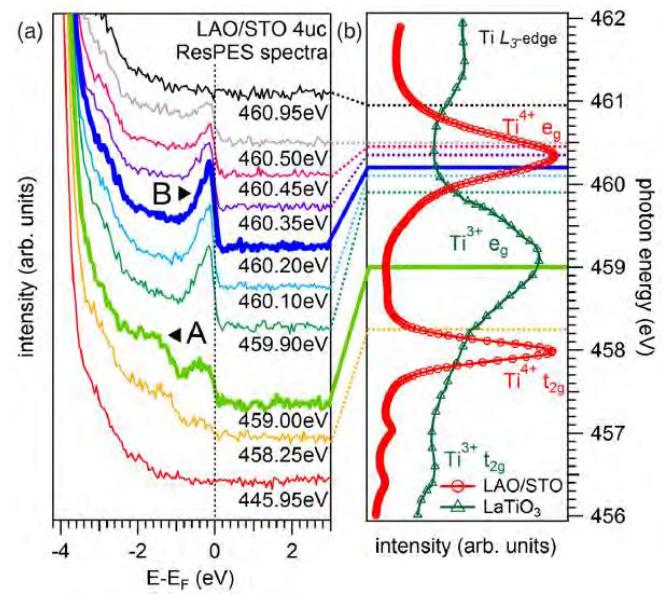
total spectrum



interface Ti spectrum



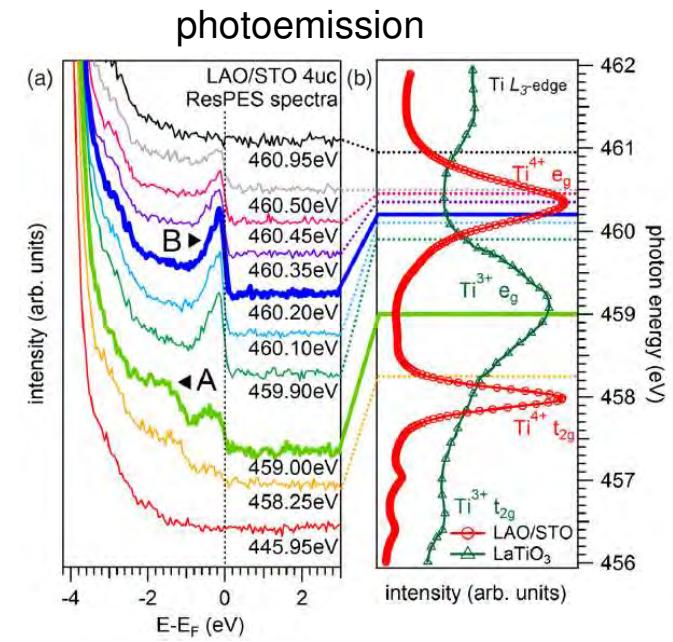
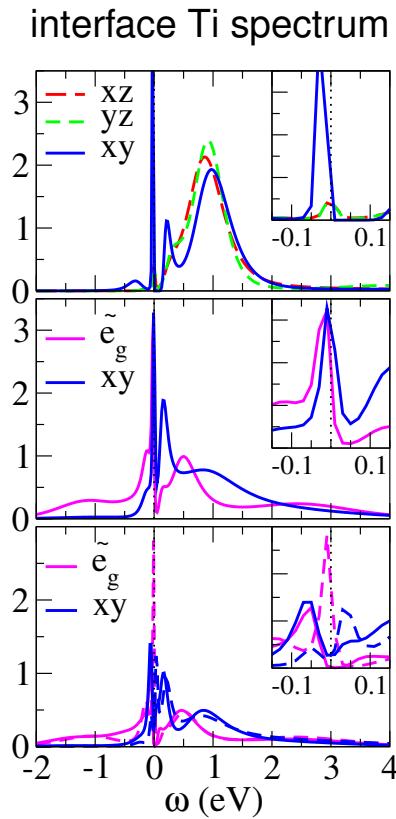
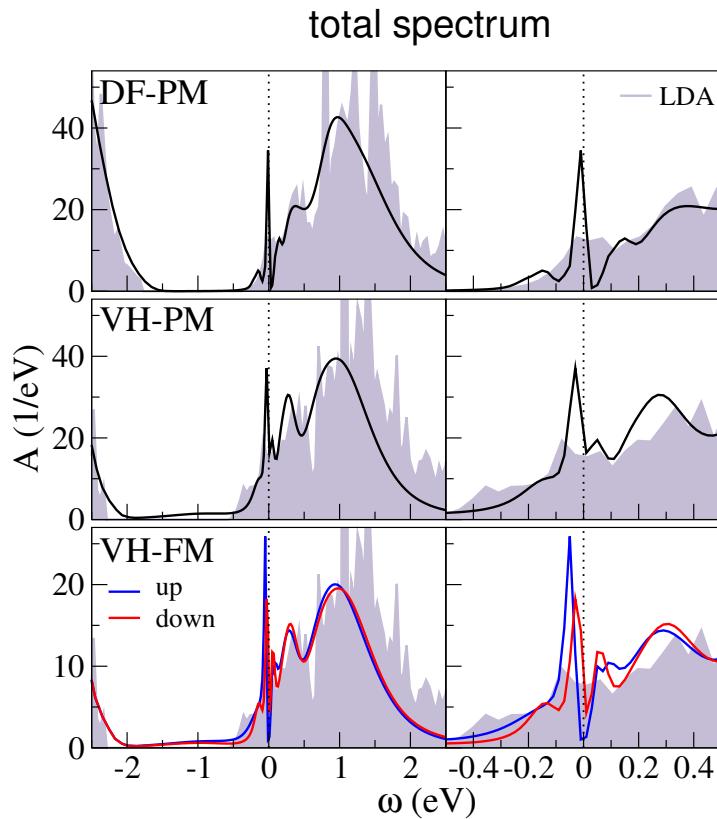
photoemission



[Cancellieri et al., PRL 110 137601 (2013)]

[Berner et al., PRL 110, 247601 (2013)]

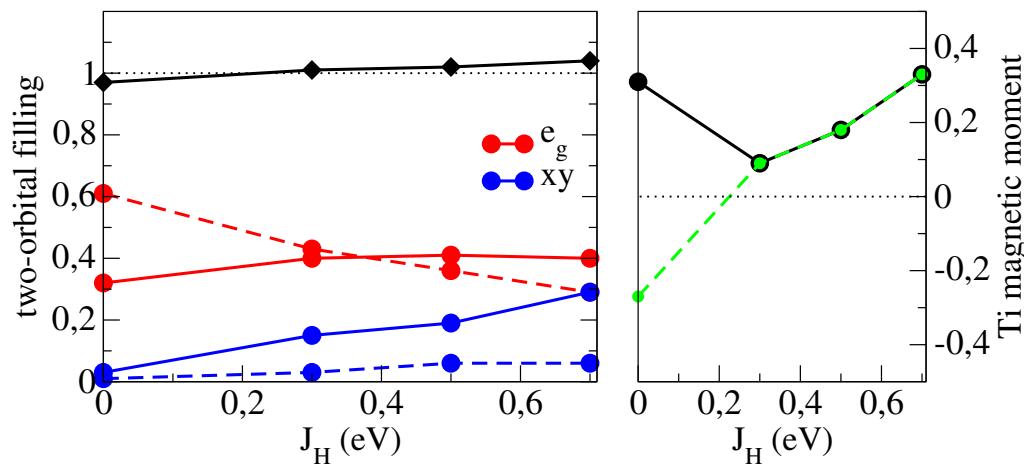
# LAO/STO dense-defect interface : DFT+DMFT



[Cancellieri et al., PRL 110 137601 (2013)]

[Berner et al., PRL 110, 247601 (2013)]

## local two-orbital fillings and polarizations with vacancies ( $U=2.5$ eV)



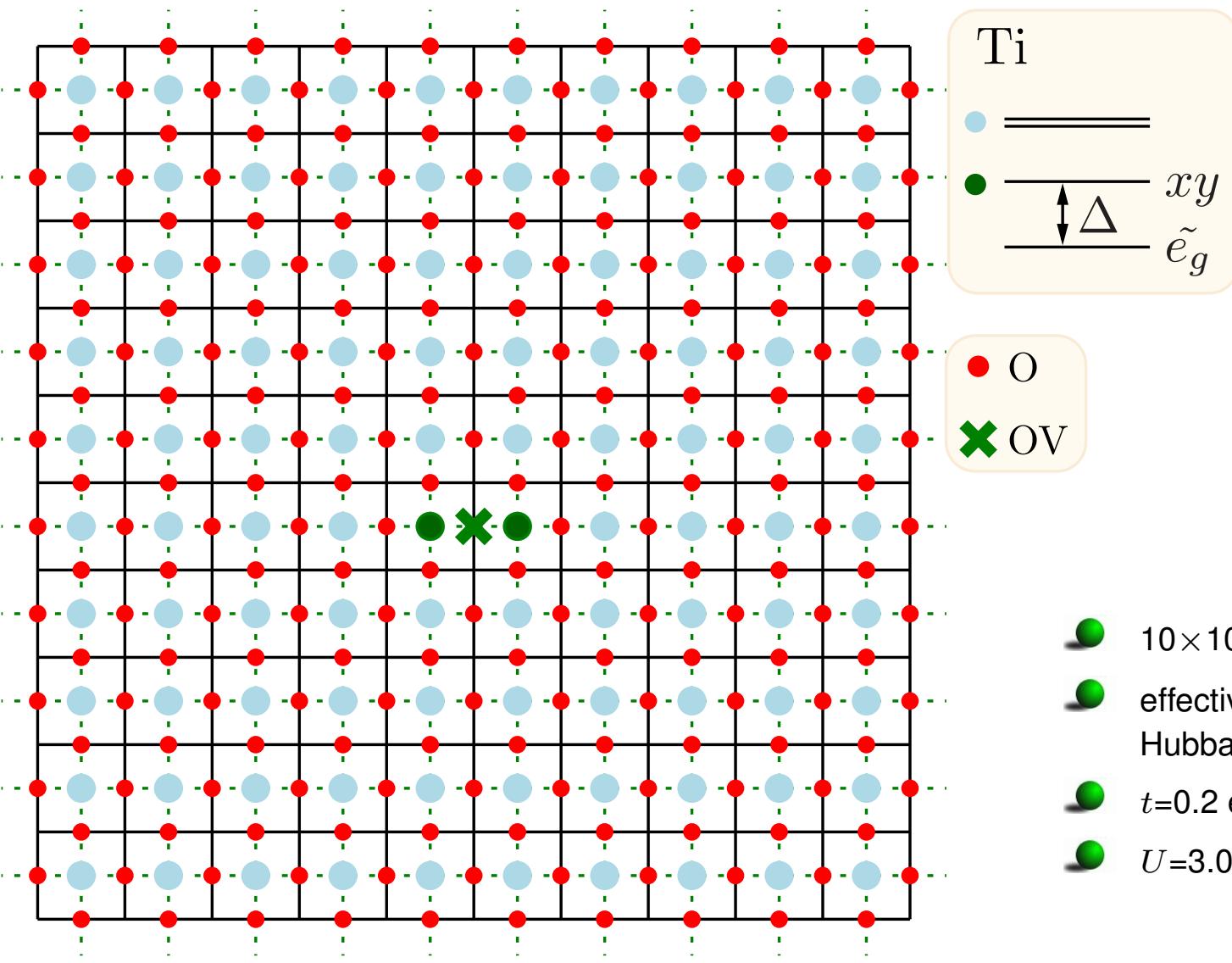
## with oxygen vacancies (VH)

- one electron at interface Ti: quarter filling
- FM moment  $m_{\text{Ti}12} \sim 0.2\mu_B$
- double-exchange mechanism
- very sensitive to  $J_H$  !

[FL, Boehnke, Grieger, Piefke, PRB 085125 (2014)]

# Arbitrary OV Concentration in LAO/STO : Real-Space Modelling

[Behrmann and FL, PRB 92, 125148 (2015)]



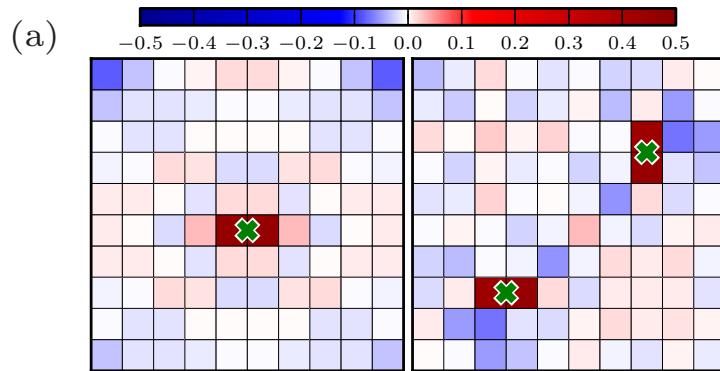
- 10×10 TiO<sub>2</sub> square lattice
- effective two-orbital Hubbard model
- $t=0.2$  eV,  $\Delta=0.3$  eV
- $U=3.0$  eV,  $J_H=0.55$  eV

Gutzwiller/Slave-Boson approach : nearest-neighbor hopping and crystal field from former DFT calculation

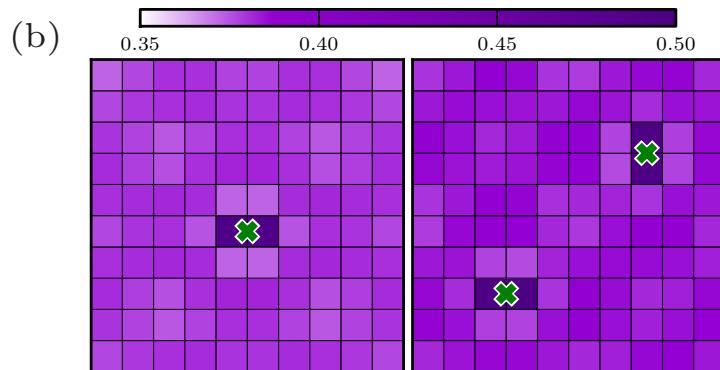
# Arbitrary OV Concentration in LAO/STO : Dilute-Defect Limit

[Behrmann and FL, PRB 92, 125148 (2015)]

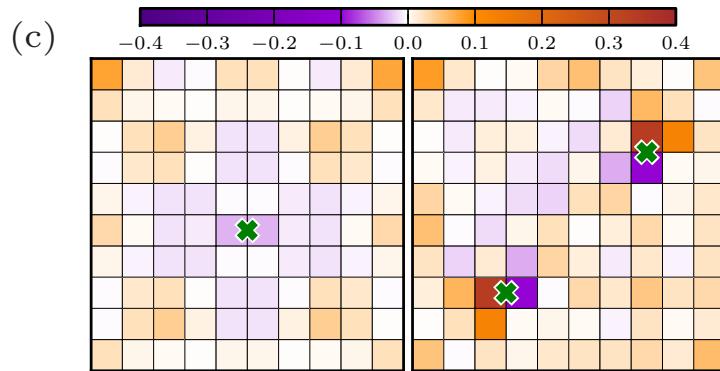
orbital  
polarization



local moment



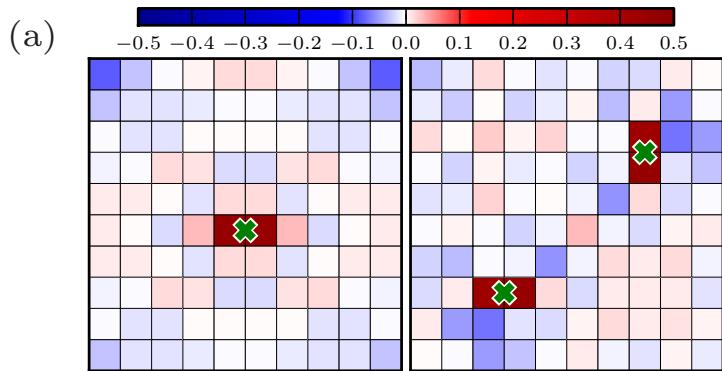
ordered  
moment



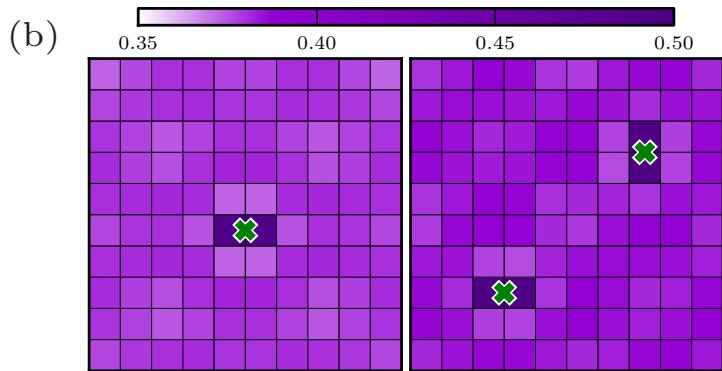
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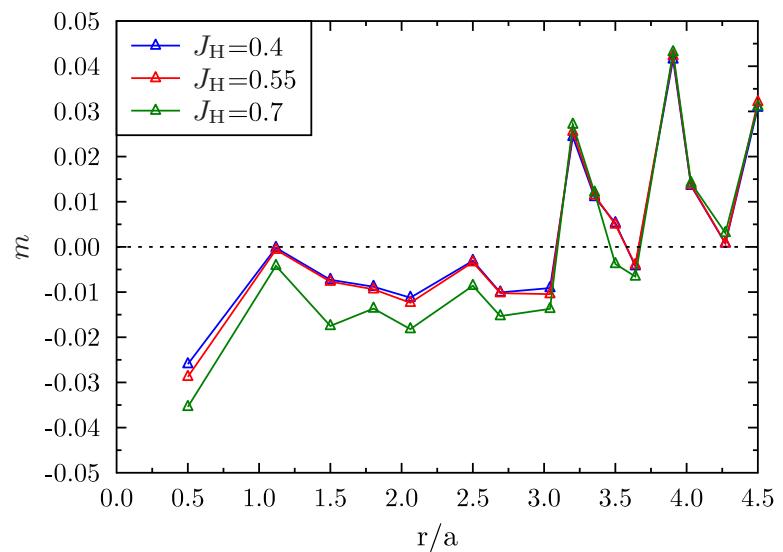
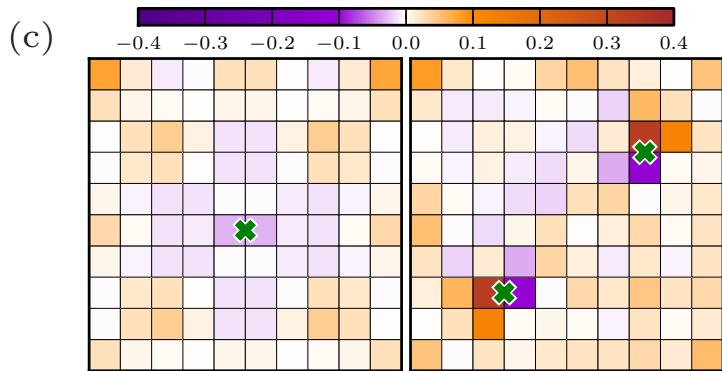
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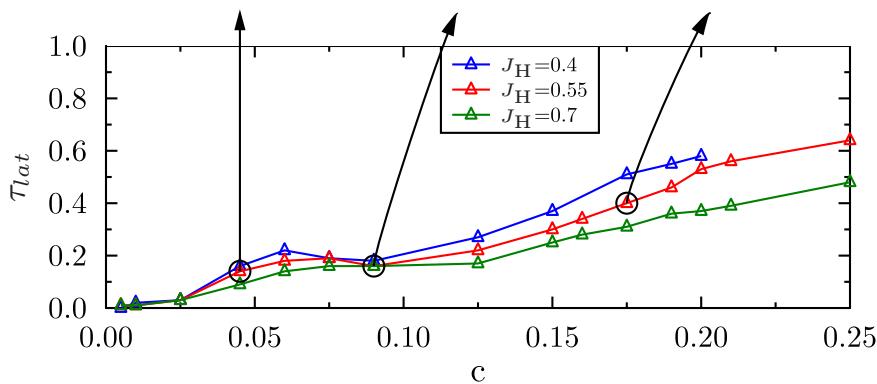
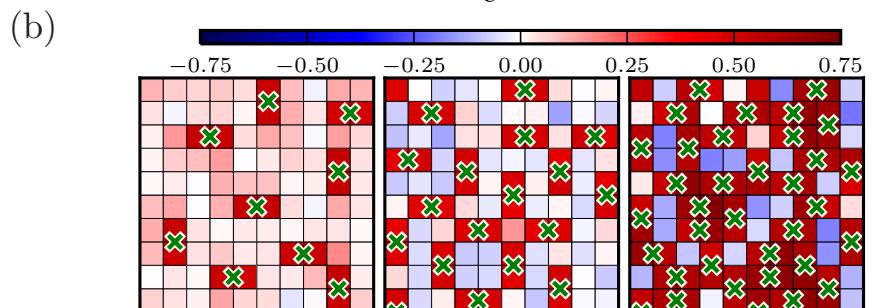
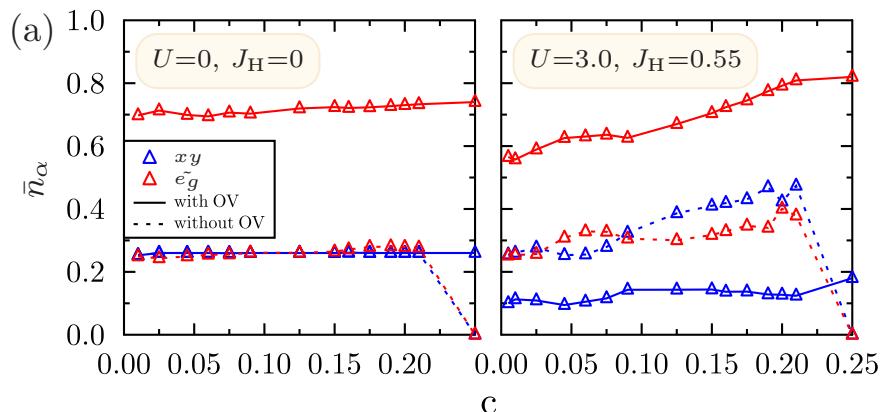
RKKY(-like) coupling

$$J(d) \cos(2k_F d) \quad , \quad d \sim 2.5 \Rightarrow k_F \sim \frac{\pi}{10}$$

→ about 1/8 filling ✓

# Arbitrary OV Concentration in LAO/STO : orbital and spin polarization

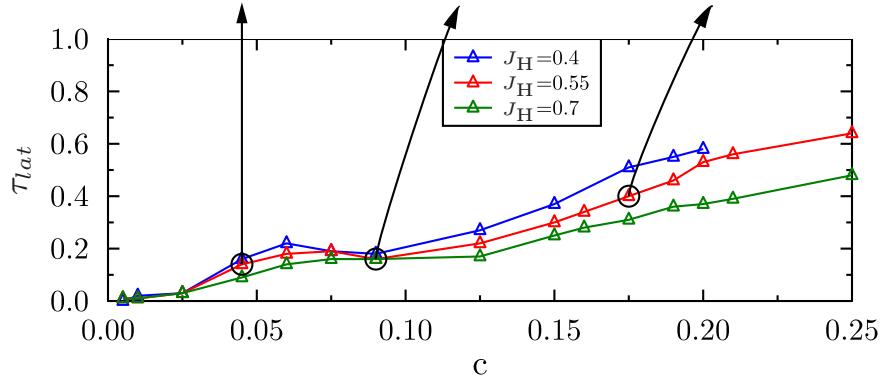
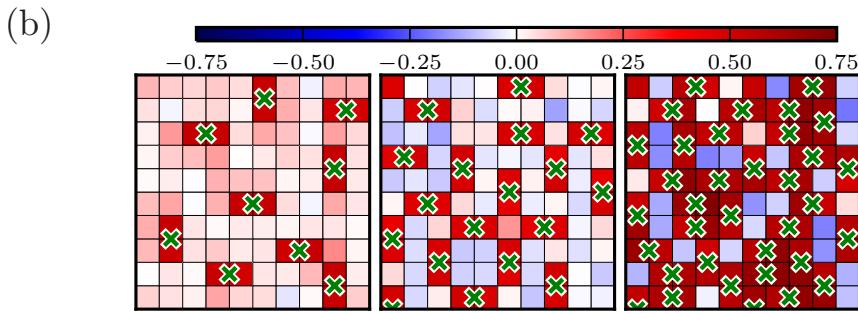
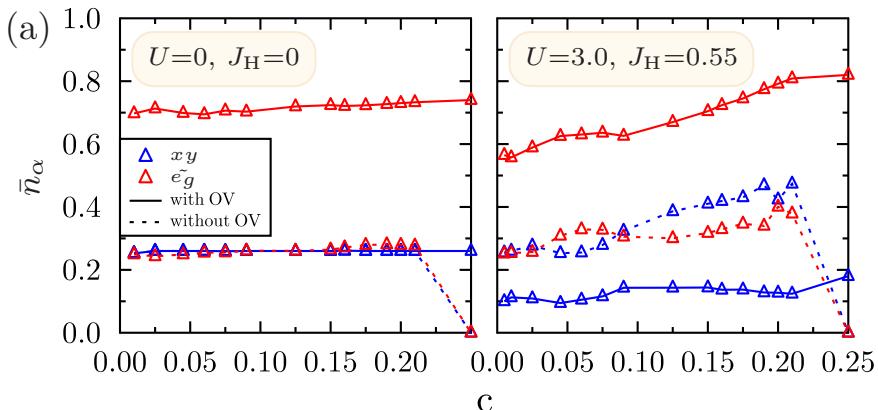
orbital occupation and orbital moment



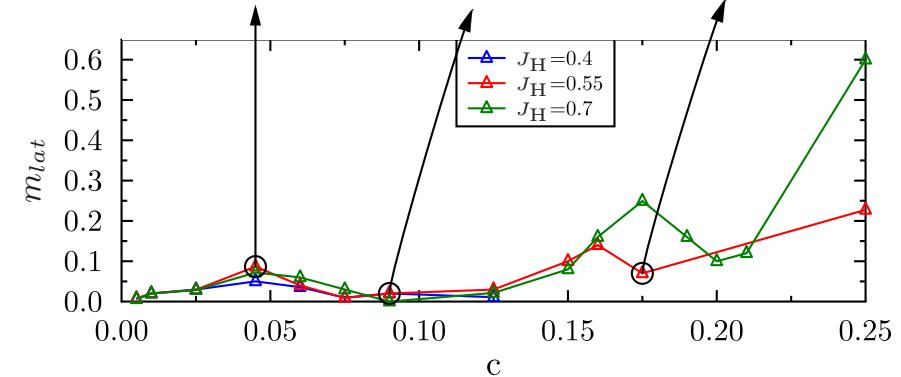
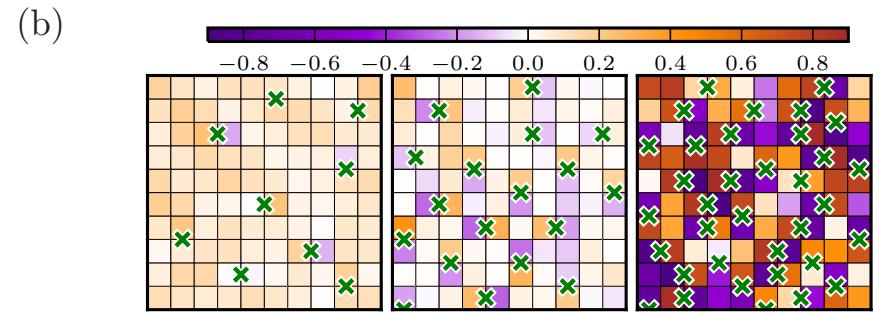
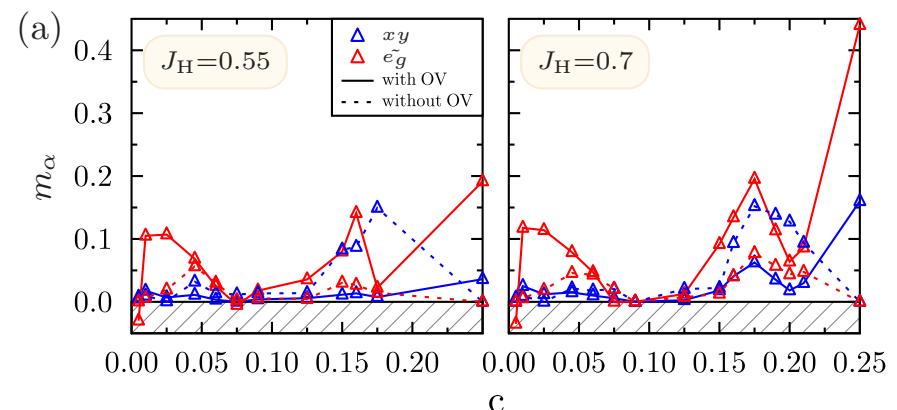
intricate dichotomy between Ti sites with and without nearby oxygen vacancies

# Arbitrary OV Concentration in LAO/STO : orbital and spin polarization

orbital occupation and orbital moment



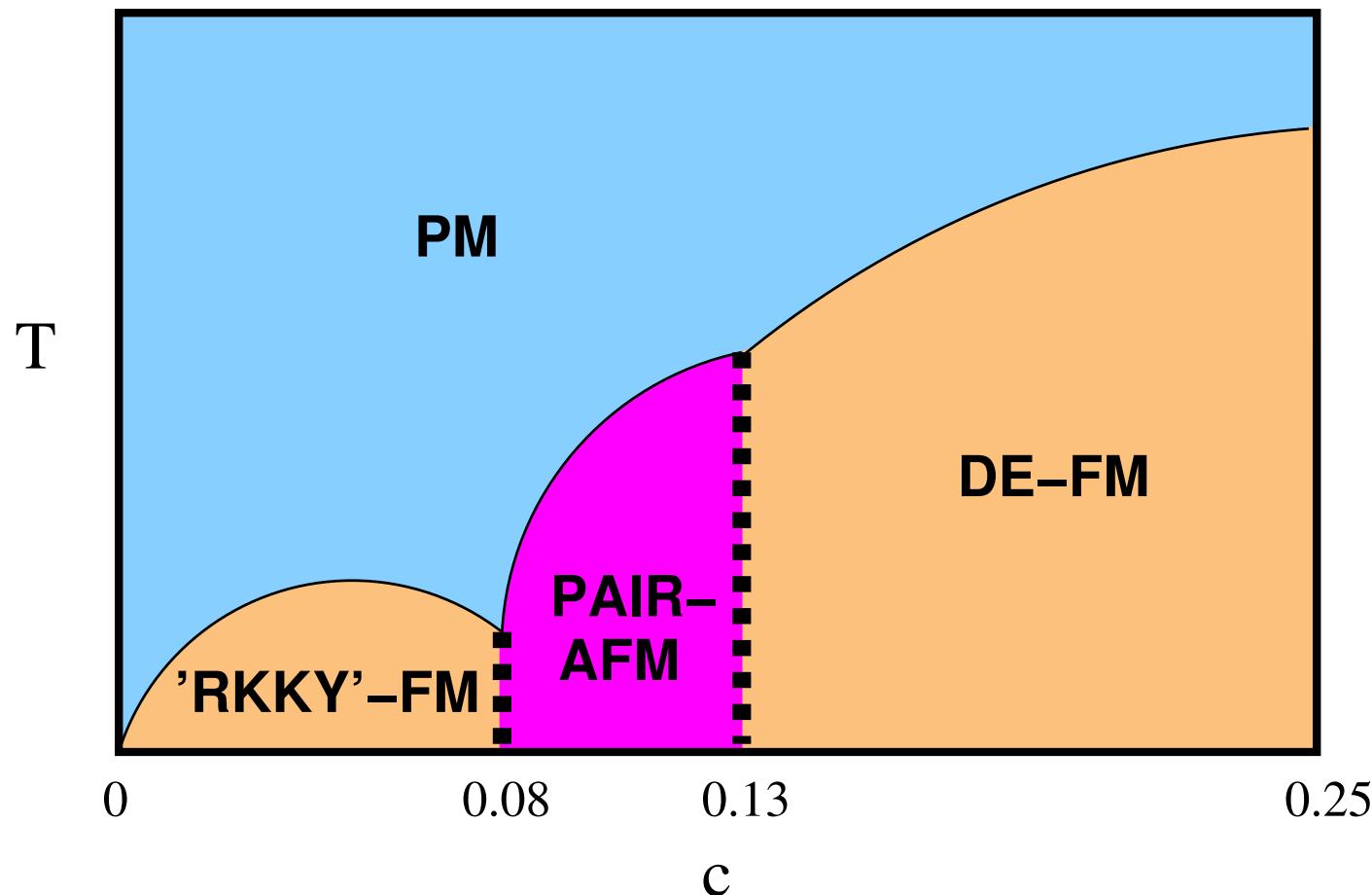
magnetic moment



intricate dichotomy between Ti sites with and without nearby oxygen vacancies

# Arbitrary OV Concentration in LAO/STO : Magnetic Phase Diagram

[Behrmann and FL, PRB 92, 125148 (2015)]

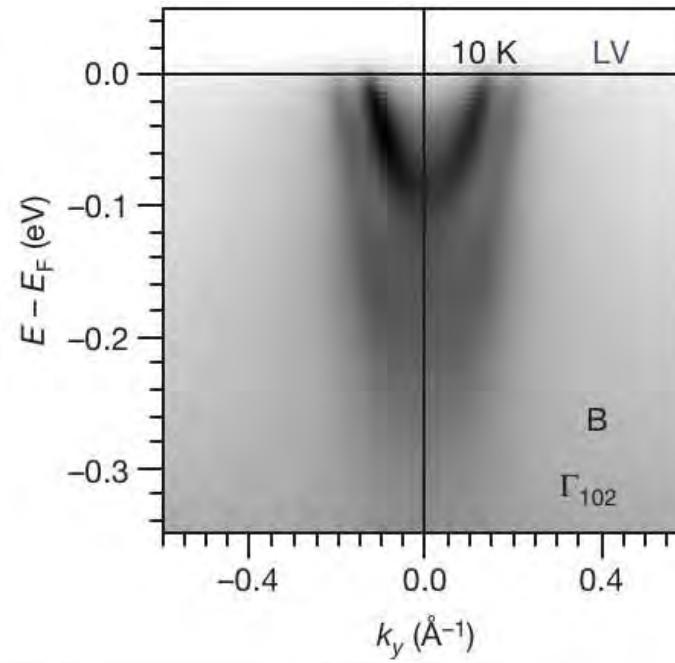
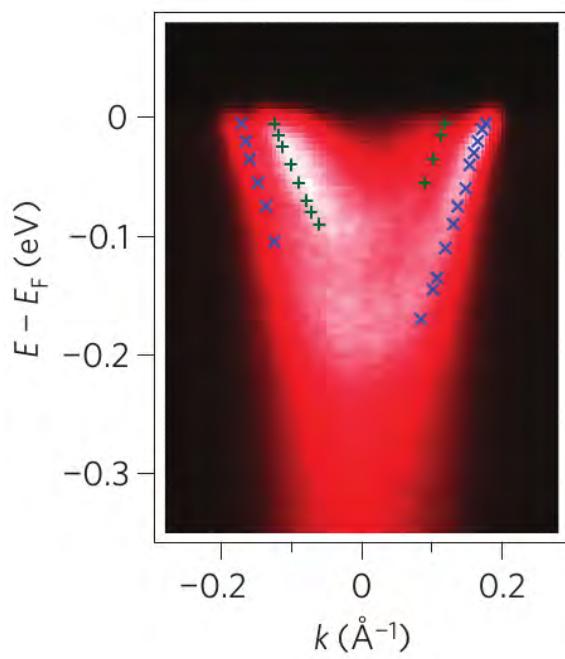
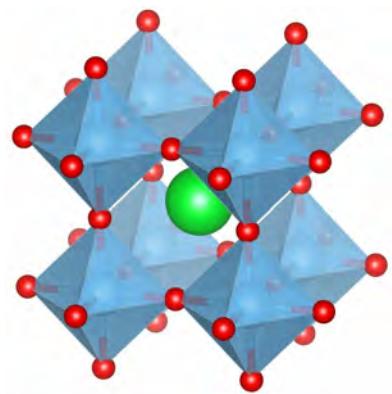


- nontrivial ferrromagnetism triggered by even few oxygen vacancies
- double-exchange-like ferromagnetism for higher oxygen vacancy concentration

And now  
for something  
completely different...



# Oxygen-Deficient SrTiO<sub>3</sub> surface : Experiment



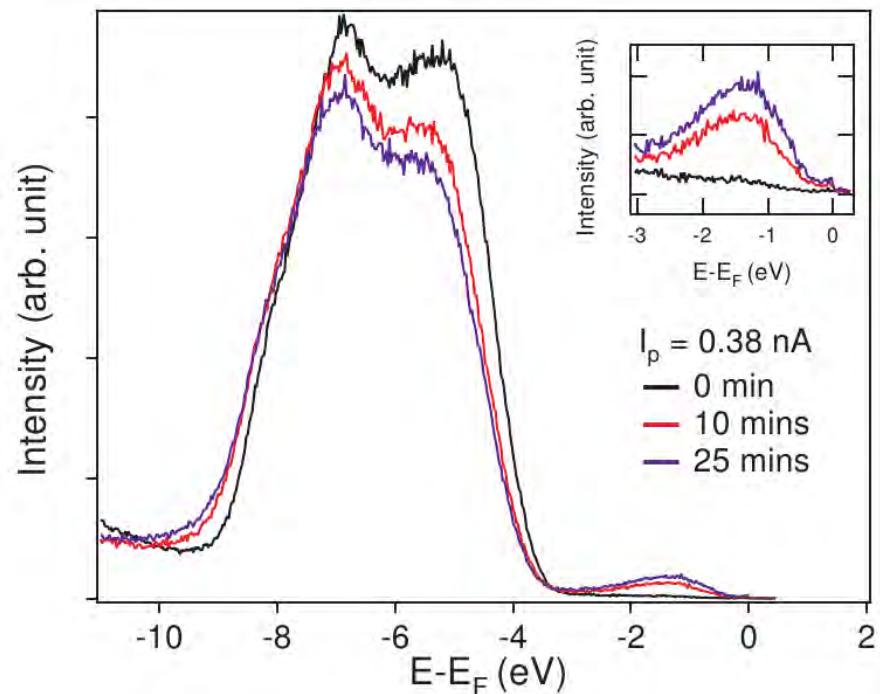
two-dimensional electron system on surface via

- exposure to UV light

[Meevasana et al., Nature Mat. 10, 114 (2011)]

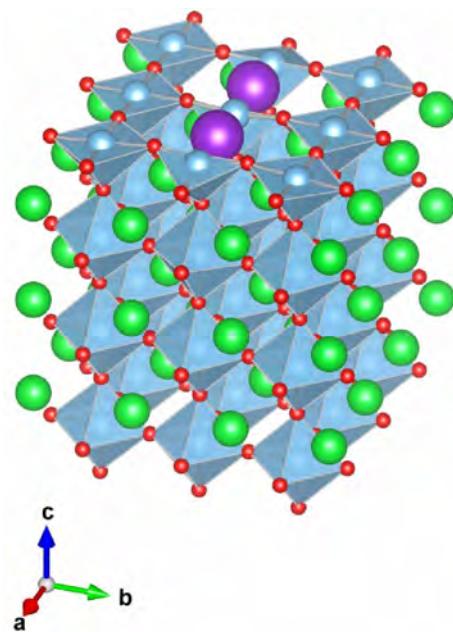
- in-situ crystal fracture

[Santander-Syro et al., Nature 469, 189 (2011)]

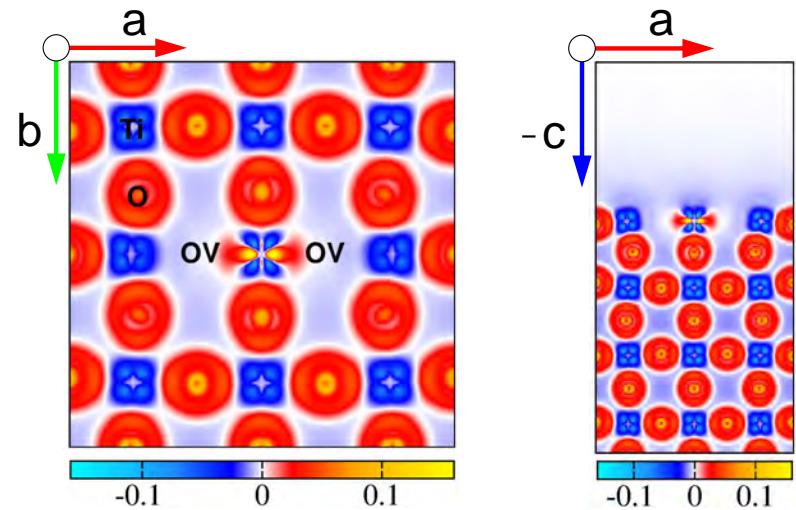


# Oxygen-Deficient SrTiO<sub>3</sub> surface : DFT+DMFT

- ★ 180-atom slab
- ★ two oxygen vacancies in TiO<sub>2</sub> surface layer
- ★ projections allow for  $e_g$  and  $t_{2g}$  states
- ★  $U=3.5\text{eV}$ ,  $J_H=0.5\text{eV}$

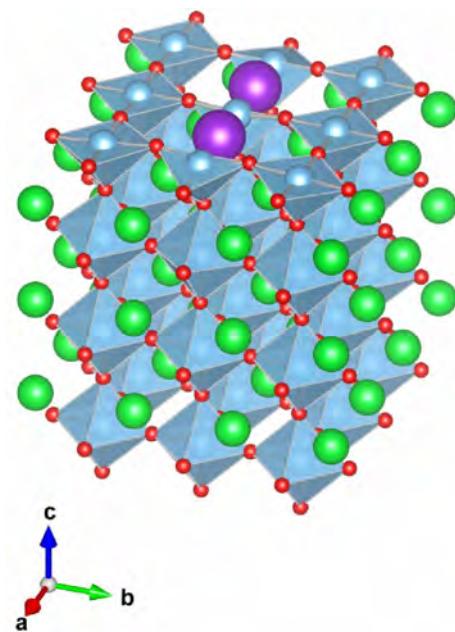


[FL, Jeschke, Kim, Backes and Valentí, PRB 93, 121103(R) (2016)]

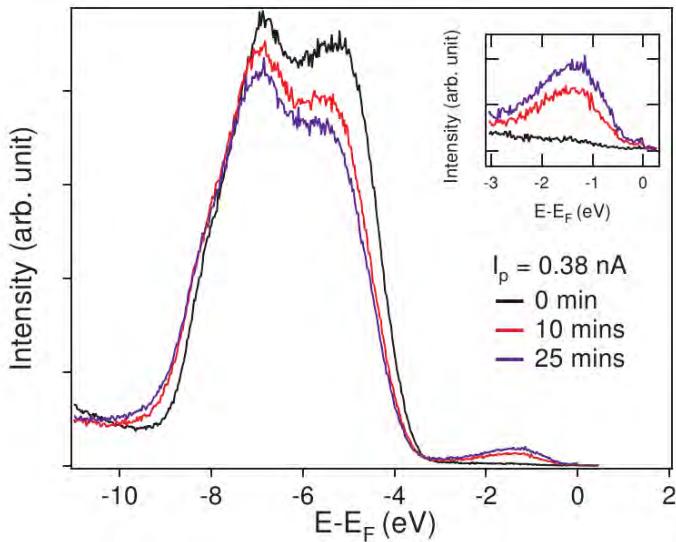
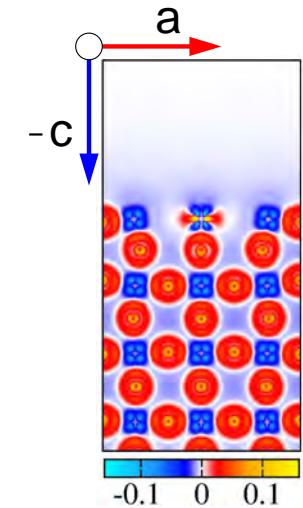
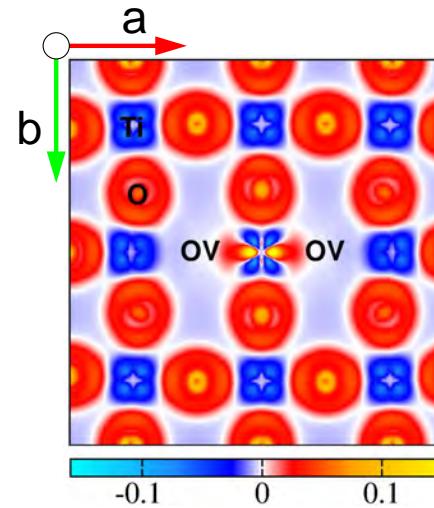


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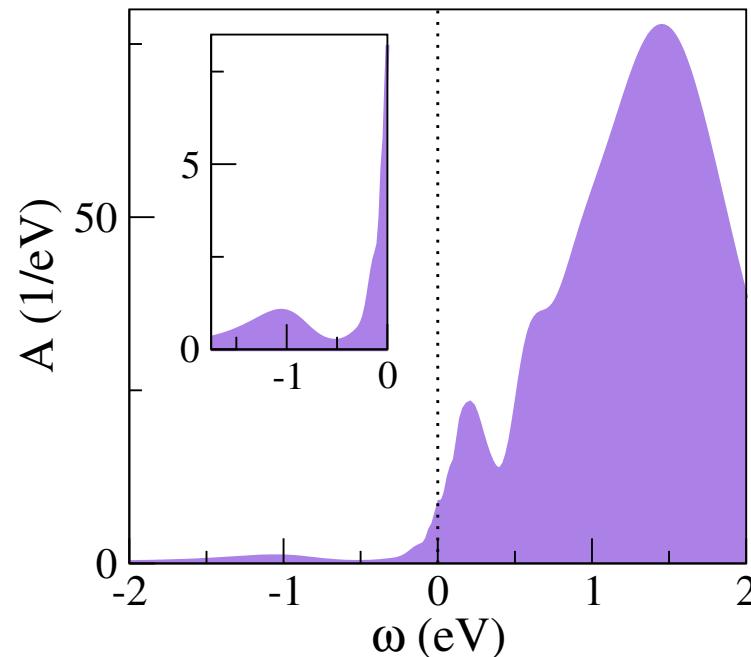
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[FL, Jeschke, Kim, Backes and Valentí, PRB 93, 121103(R) (2016)]



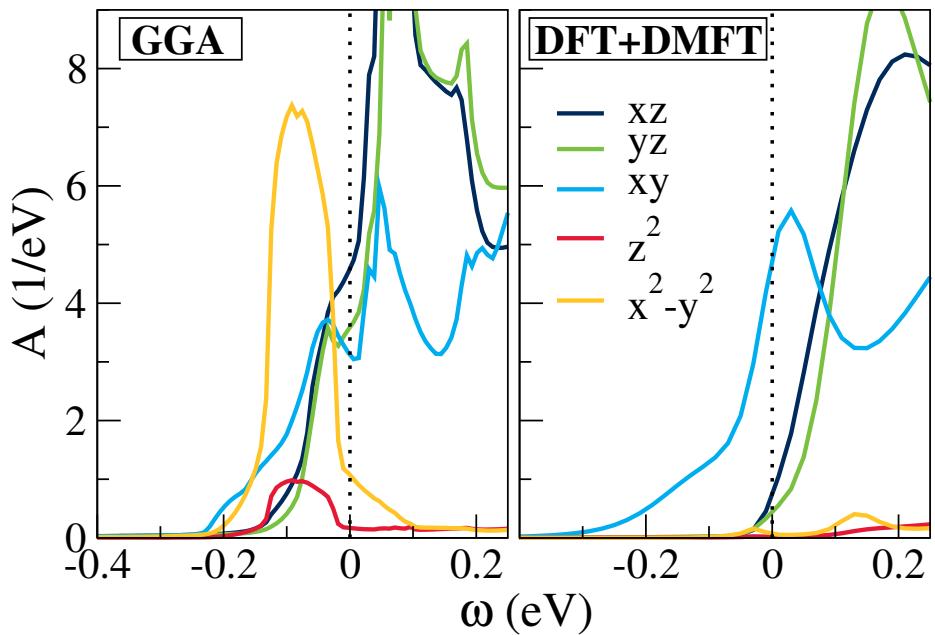
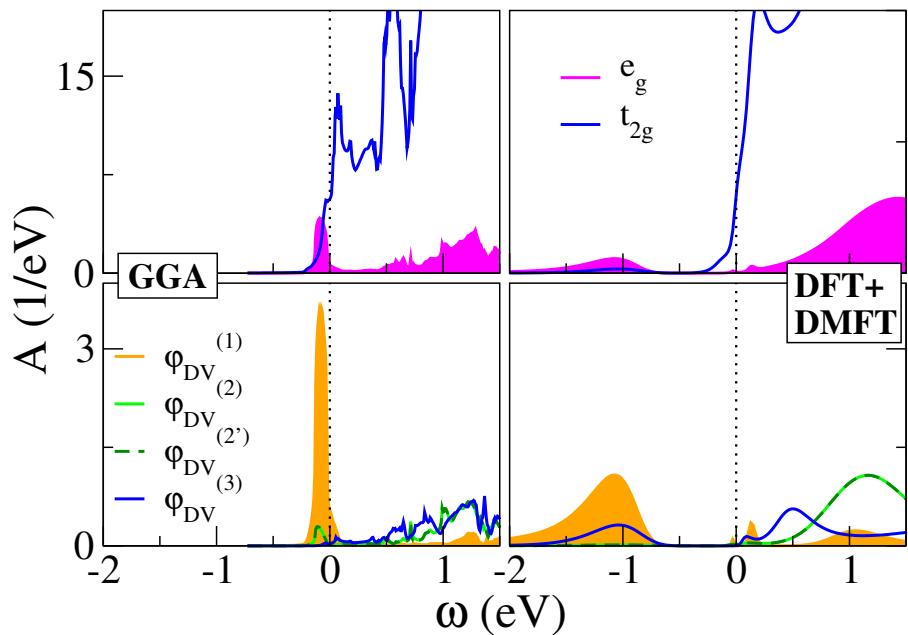
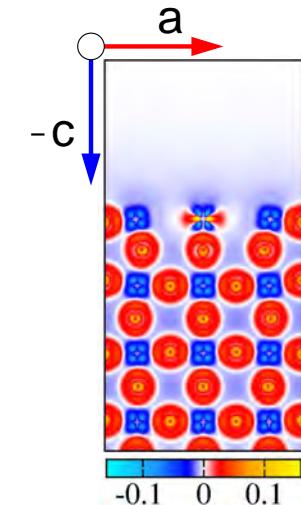
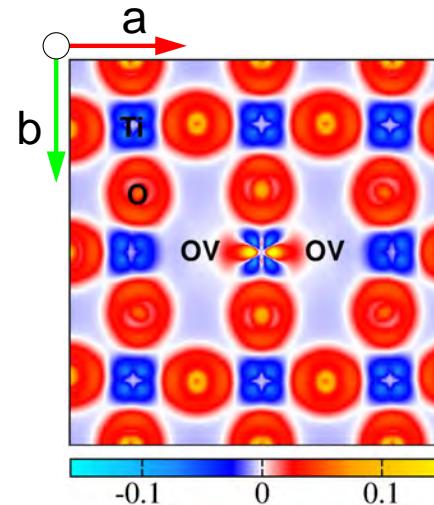
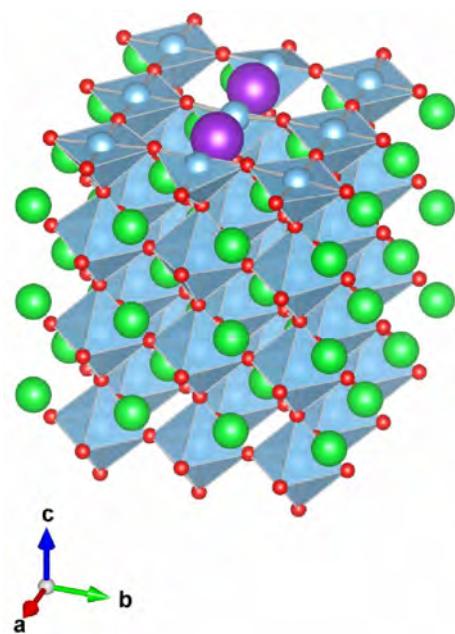
[Meevasana et al., Nature Mat. 10, 114 (2011)]



# Oxygen-Deficient SrTiO<sub>3</sub> surface : DFT+DMFT

[FL, Jeschke, Kim, Backes and Valentí, PRB 93, 121103(R) (2016)]

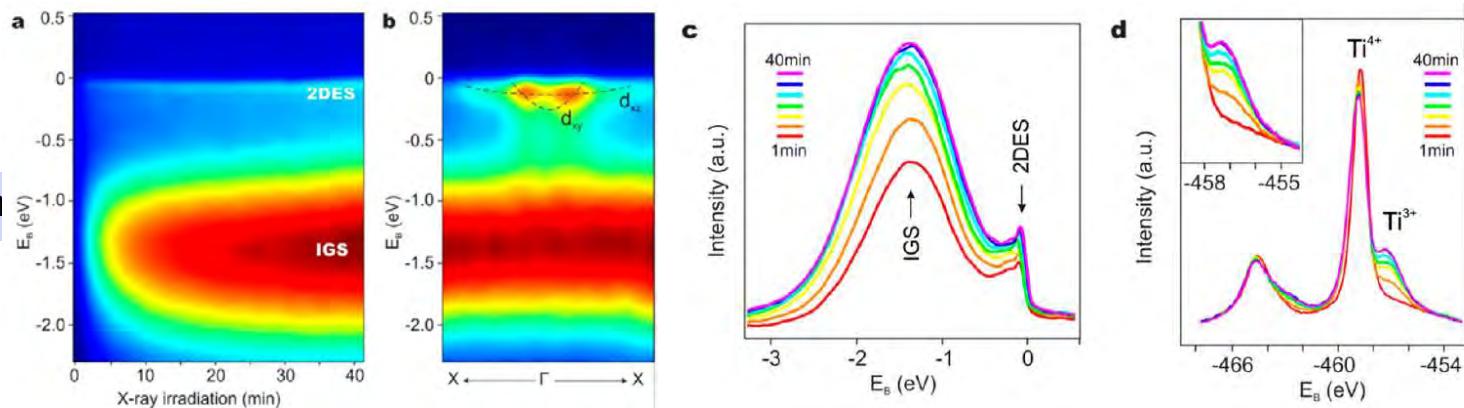
- \* 180-atom slab
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- \* projections allow for  $e_g$  and  $t_{2g}$  states
- \*  $U=3.5\text{eV}$ ,  $J_H=0.5\text{eV}$



# LaAlO<sub>3</sub>/SrTiO<sub>3</sub> revisited : experiment and DFT+DMFT

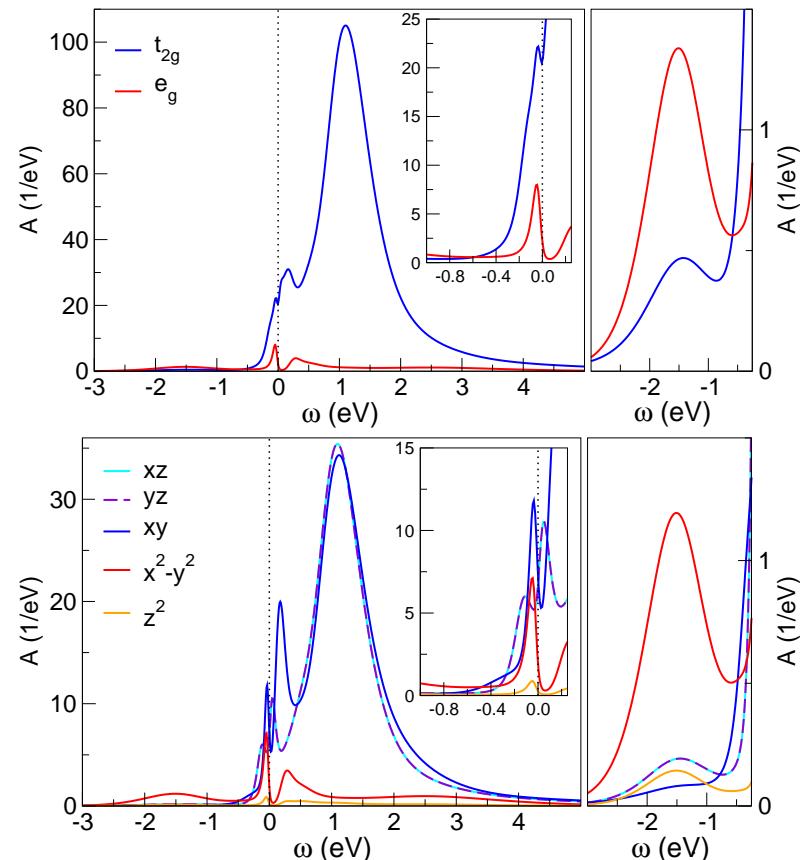
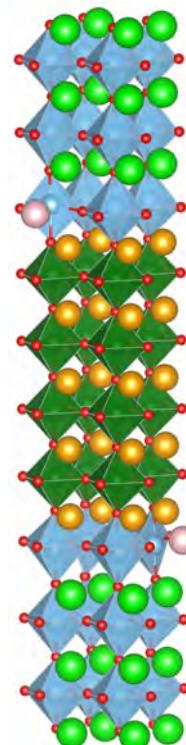
[FL, Boehnke, Grieger and Piefke, PRB 90, 085125 (2014)] [Chikina, FL, Husanu et al., ACS Nano 12, 7927 (2018)]

## experimental spectrum



## theoretical description

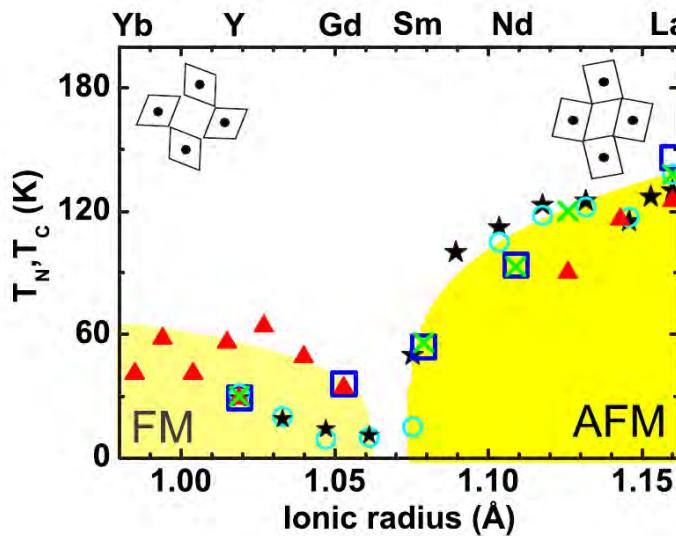
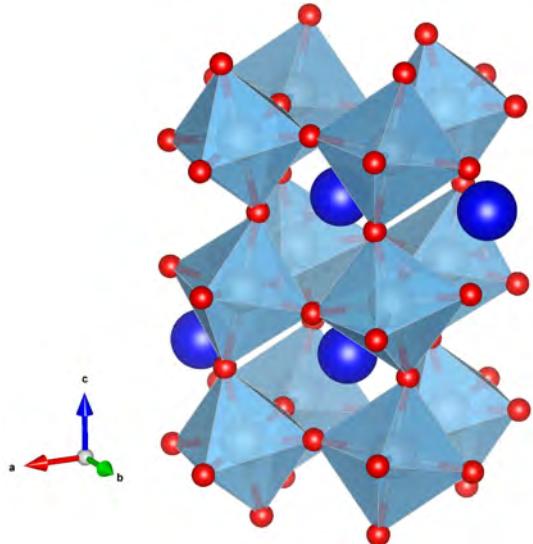
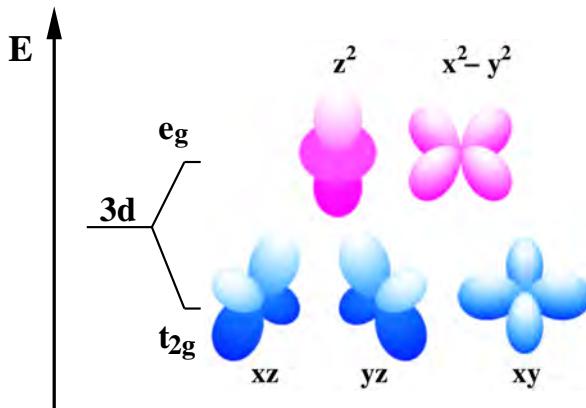
- 200-atom supercell
- Hubbard  $U = 3$  eV,  
Hund's exchange  $J_H = 0.5$  eV



# Doping the Mott-Insulating State : Phenomenology of Bulk Titanates

Mott-insulating distorted perovskites  $RTiO_3$

→ Ti<sup>3+</sup> with  $3d^1(t_{2g})$



[Komarek et al., PRB 75, 224402 (2007)]

LaTiO<sub>3</sub>

AFM  $T_N=146\text{K}$ , apical tilt  $\Theta=13^\circ$ , charge gap  $\Delta=0.20\text{ eV}$

GdTiO<sub>3</sub>

FM  $T_C=36\text{K}$ , apical tilt  $\Theta=18^\circ$ , charge gap  $\Delta=0.75\text{ eV}$

SmTiO<sub>3</sub>

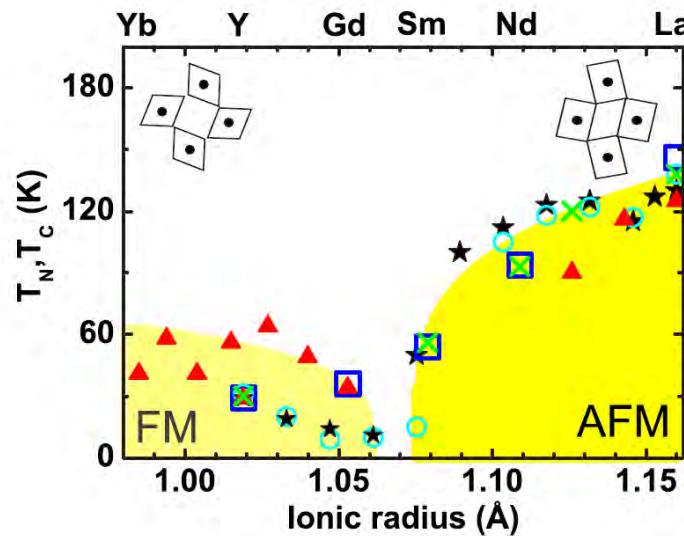
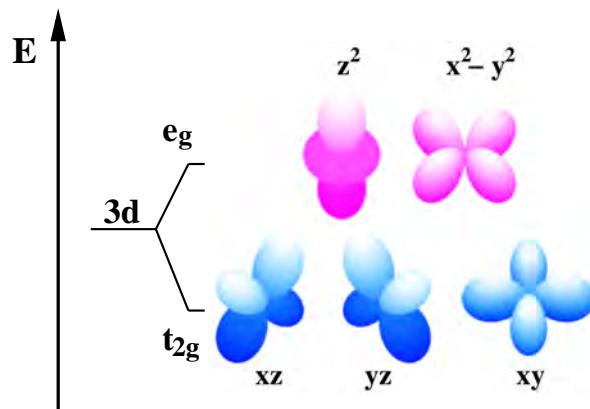
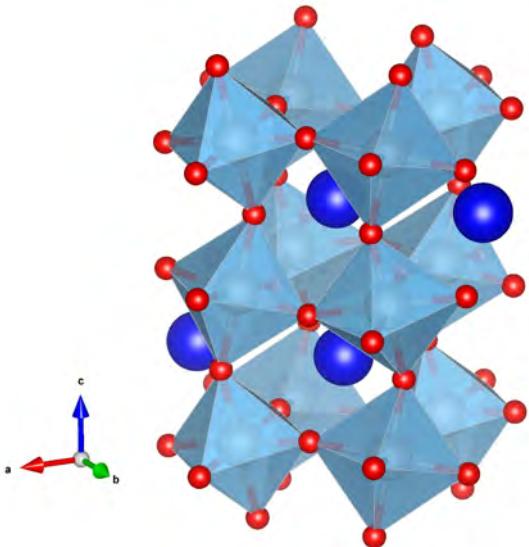
AFM  $T_N=48\text{K}$ , apical tilt  $\Theta=17^\circ$ , charge gap  $\Delta=0.50\text{ eV}$

[Crandles et al., Physica C, 407 (1992)] [Okimoto et al., PRB 95, 9581 (1995)]

# Doping the Mott-Insulating State : Phenomenology of Bulk Titanates

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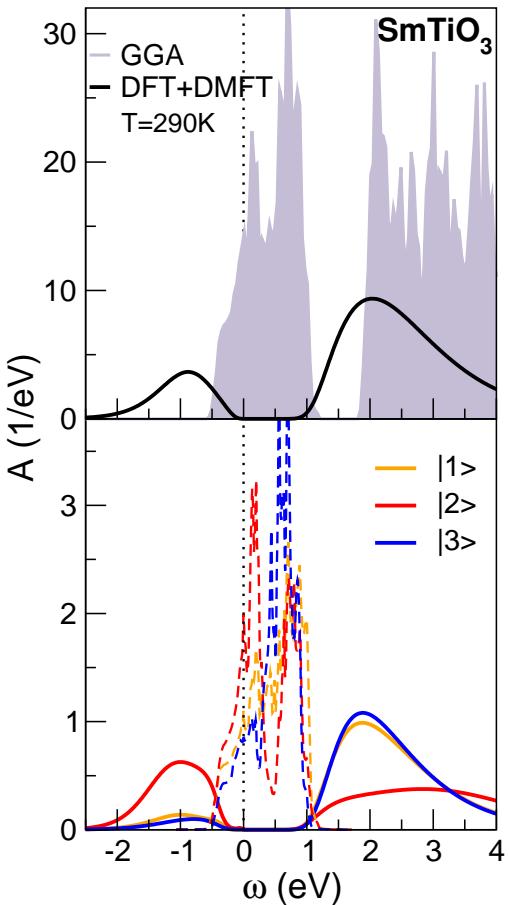
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SmTiO<sub>3</sub>

AFM  $T_N=48\text{K}$ , apical tilt  $\Theta=17^\circ$ , charge gap  $\Delta=0.50\text{ eV}$

[Crandles et al., Physica C, 407 (1992)] [Okimoto et al., PRB 95, 9581 (1995)]

$U=5\text{ eV}$   $J_H=0.64\text{ eV}$

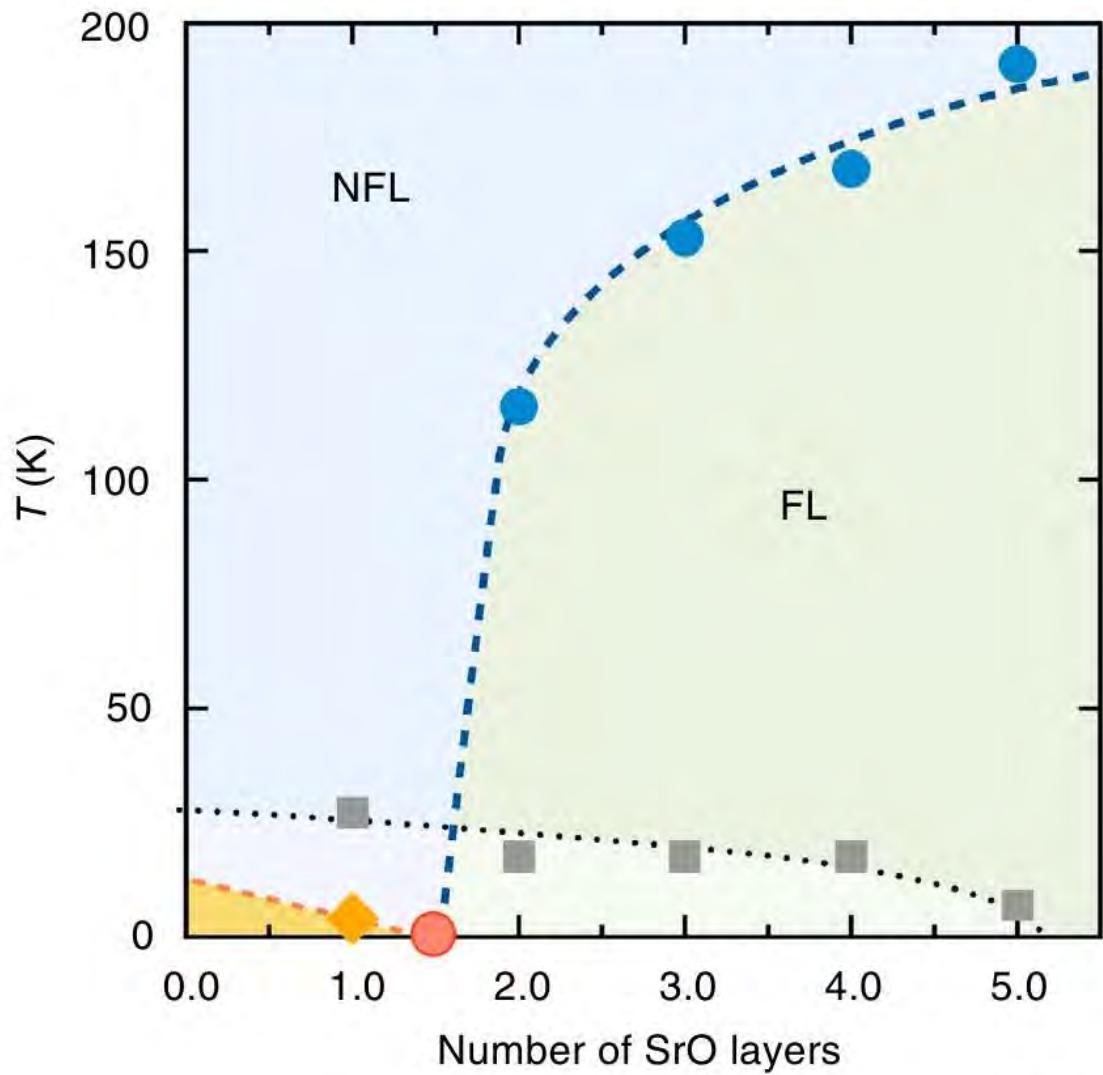
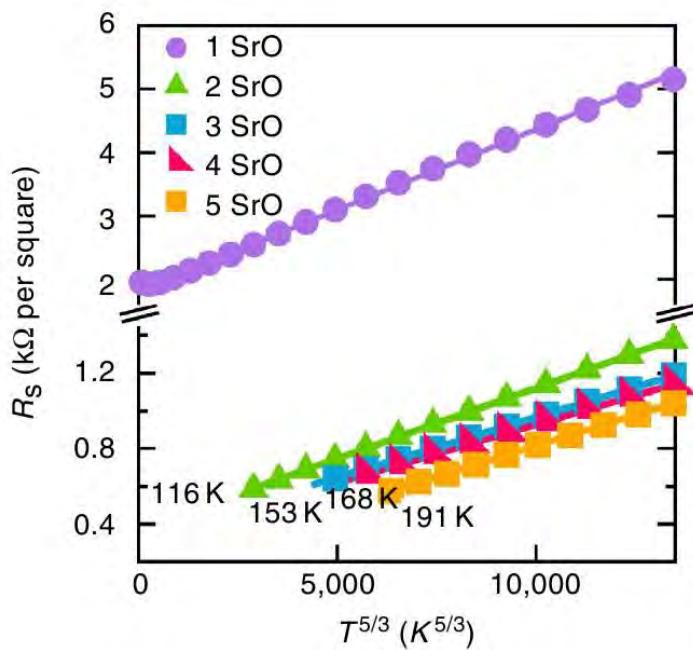
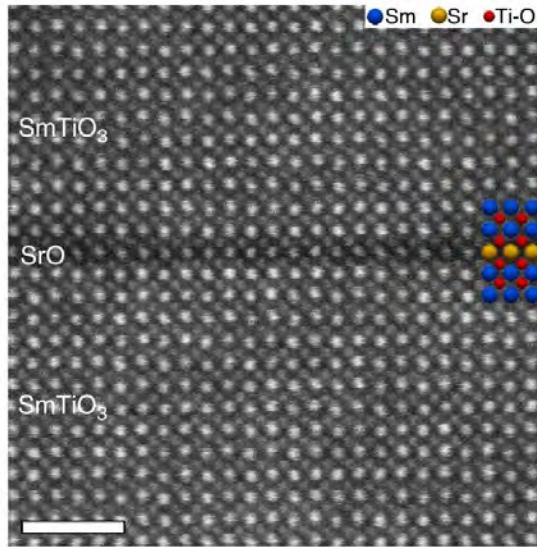


SmTiO<sub>3</sub> is close to an AFM-to-FM quantum phase transition

# $\delta$ -doped SmTiO<sub>3</sub> : Experimental Non-Fermi-Liquid Behavior

[Jackson et al., Nat. Commun. 5, 4258 (2014)]

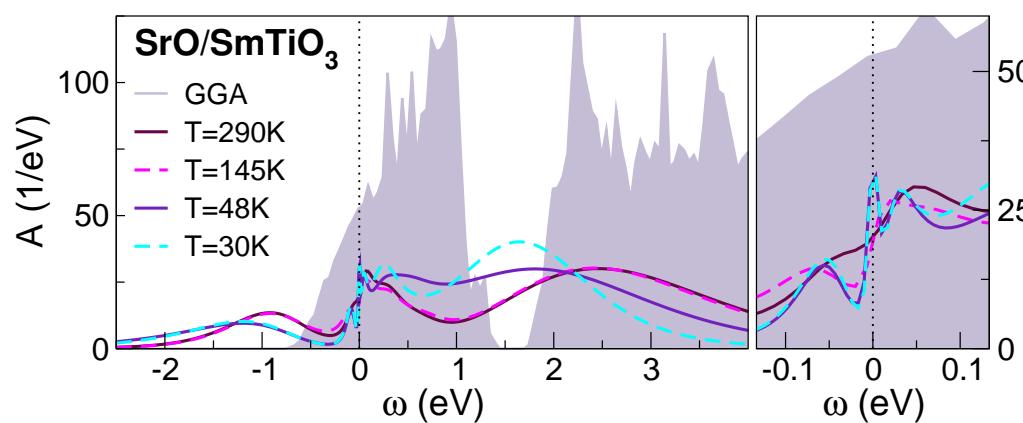
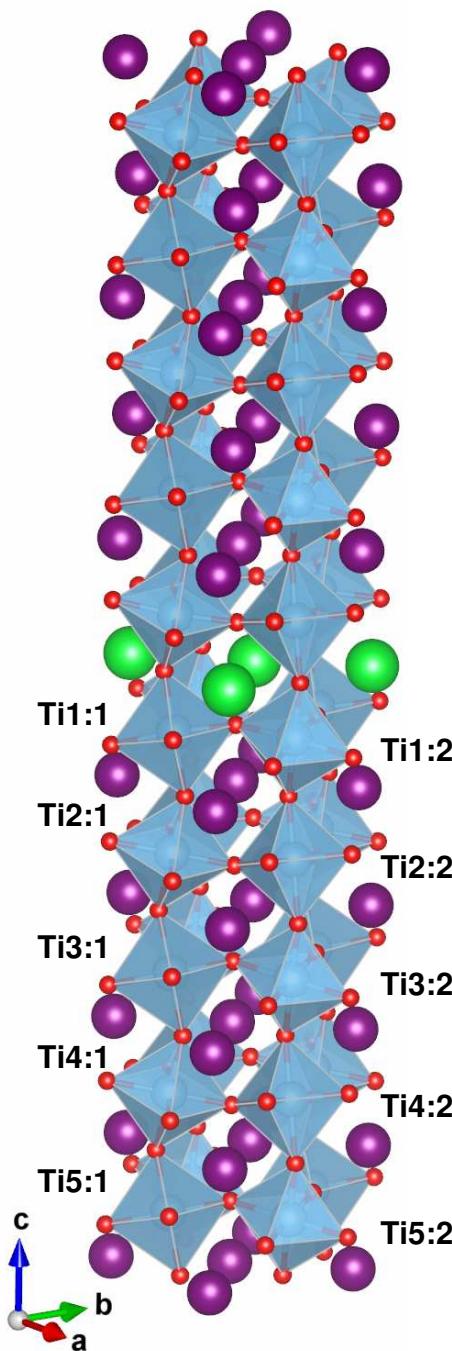
well-defined doping with layers of SrO through molecular-beam epitaxy



$T^{5/3}$ -law for the resistivity

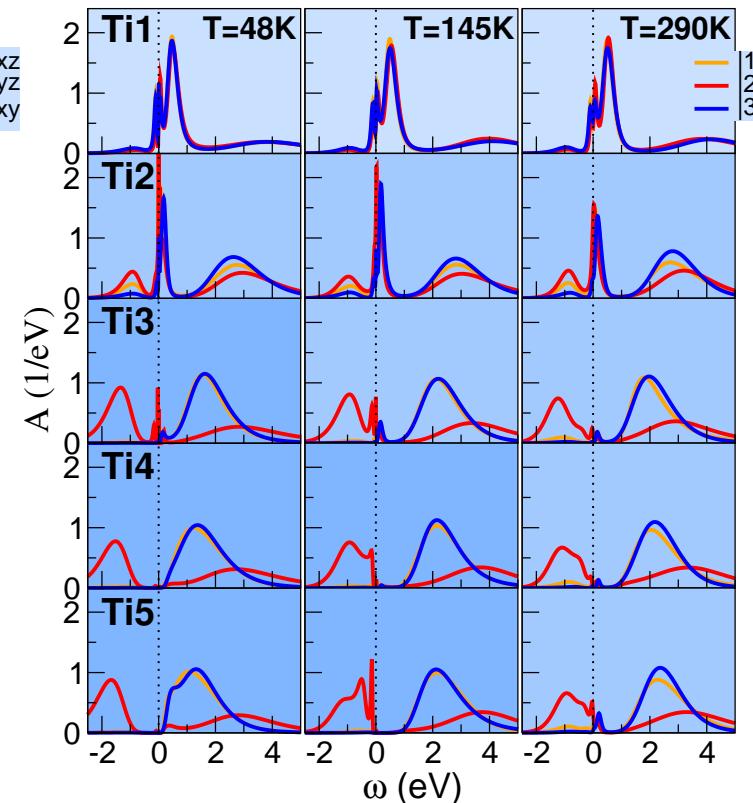
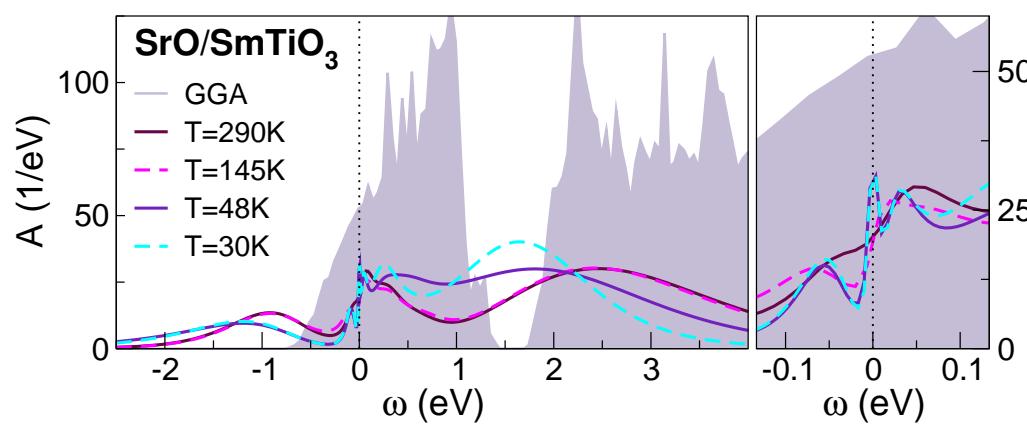
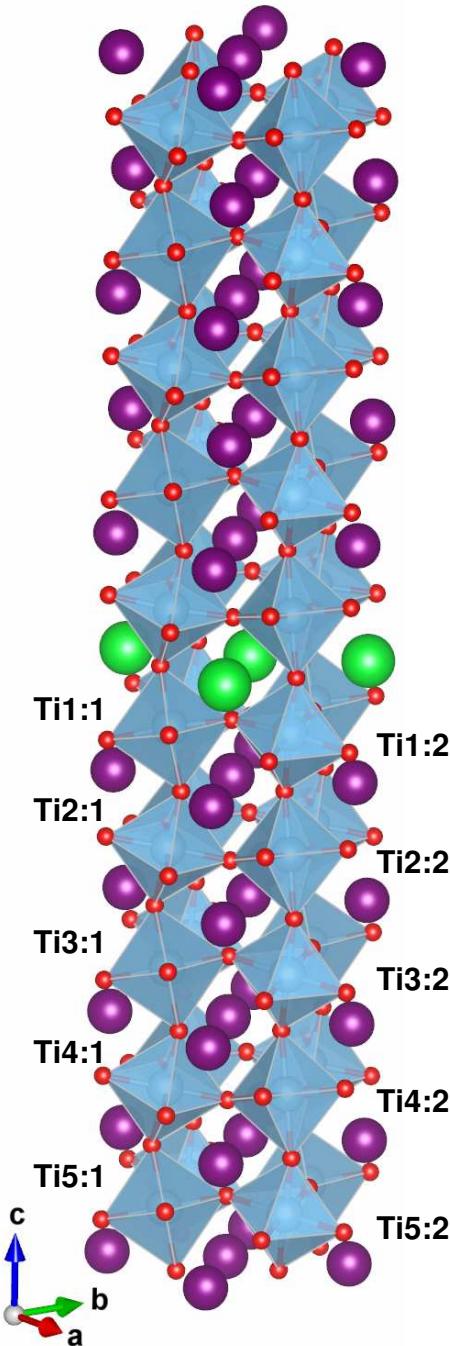
# $\delta$ -doped SmTiO<sub>3</sub> : Spectral Function from DFT+DMFT

[FL, Sci. Rep. 7, 1565 (2017)]



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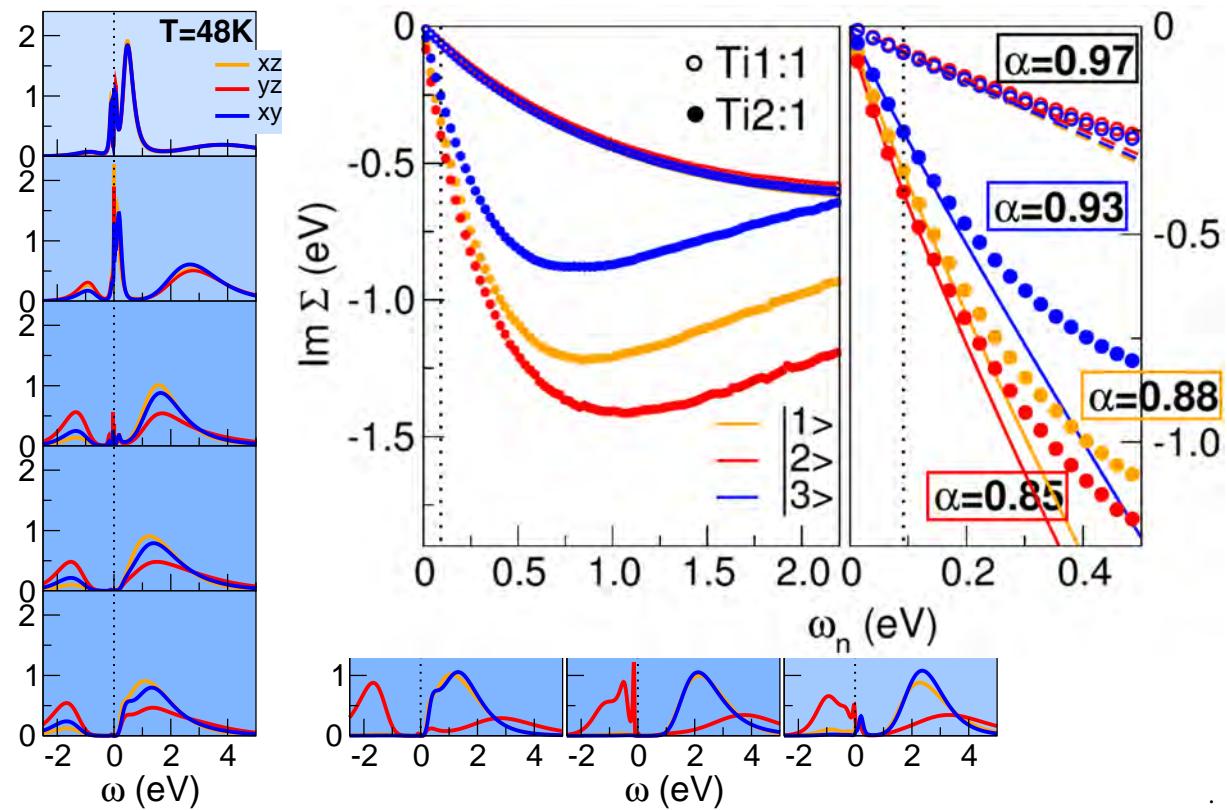
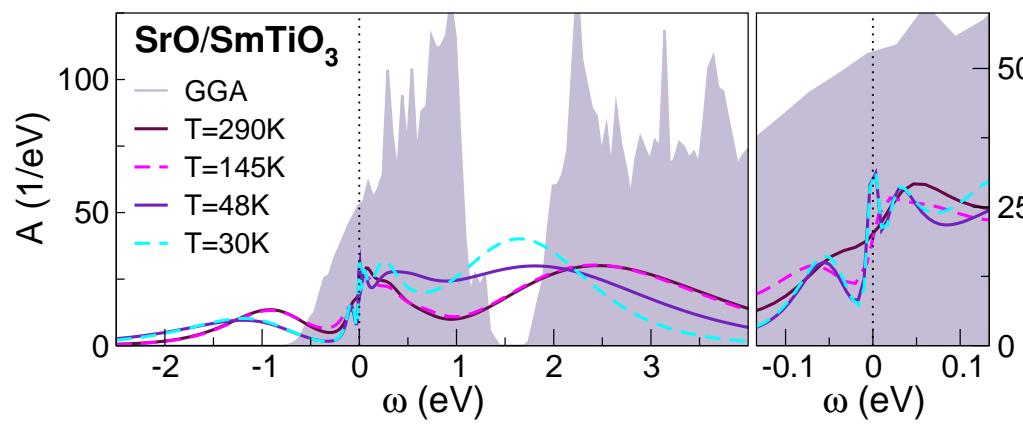
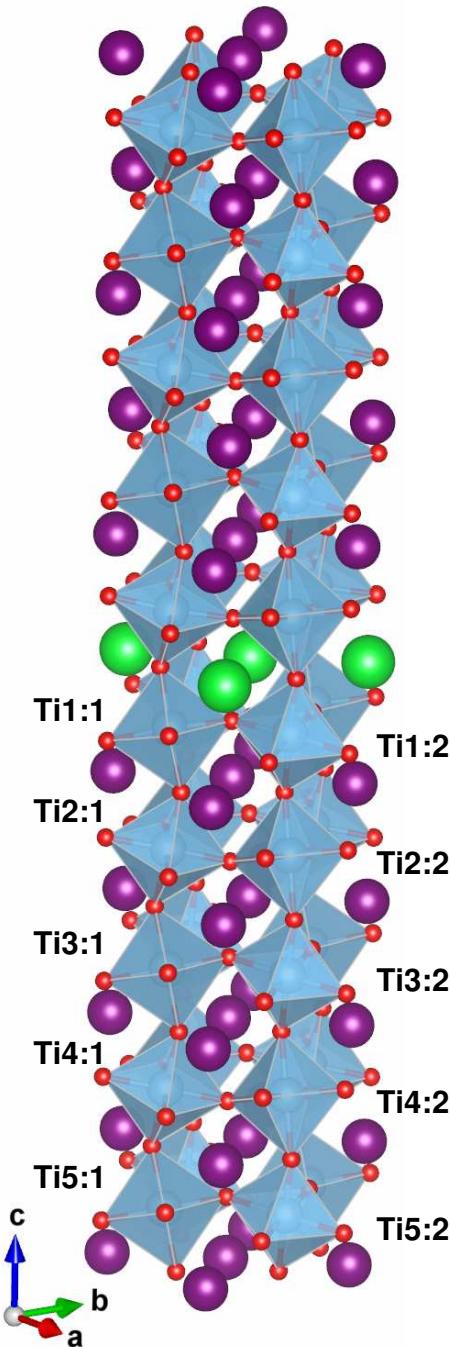
[FL, Sci. Rep. 7, 1565 (2017)]



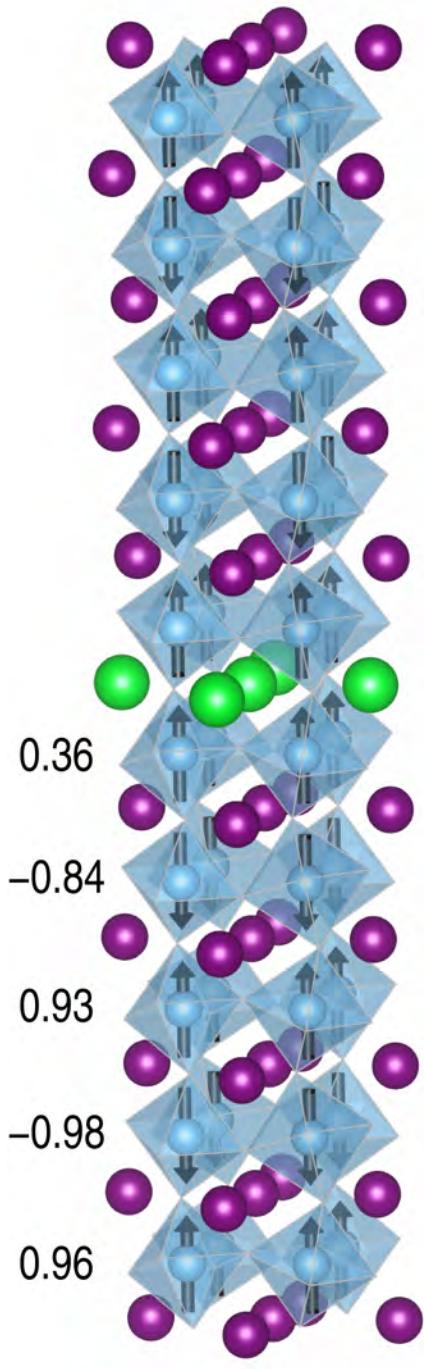
↓  
layer-dependent  
multi-orbital  
Mott transition

# $\delta$ -doped SmTiO<sub>3</sub> : Spectral Function from DFT+DMFT

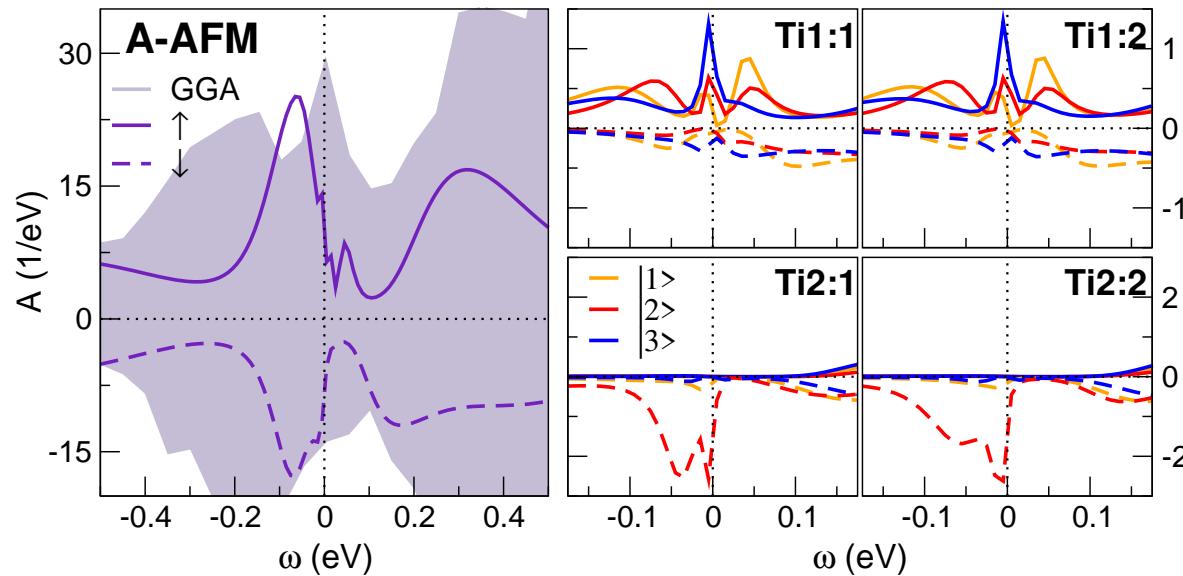
[FL, Sci. Rep. 7, 1565 (2017)]



# $\delta$ -doped SmTiO<sub>3</sub> : Magnetic Order and Pseudogap Fingerprint

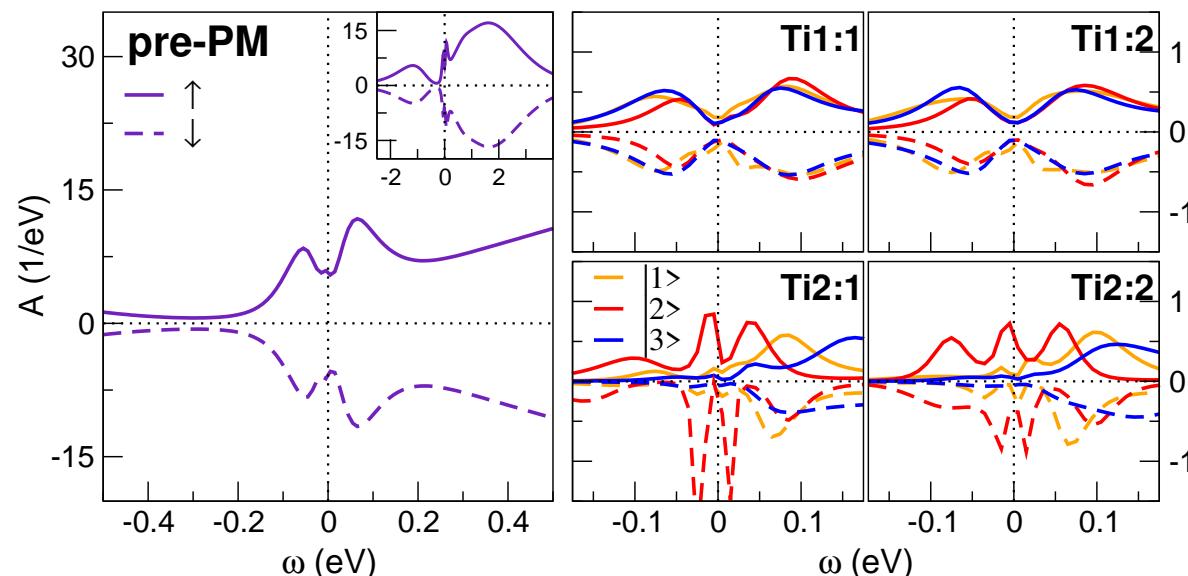


A-type AFM phase



pre-converged PM phase

with pseudogap signature



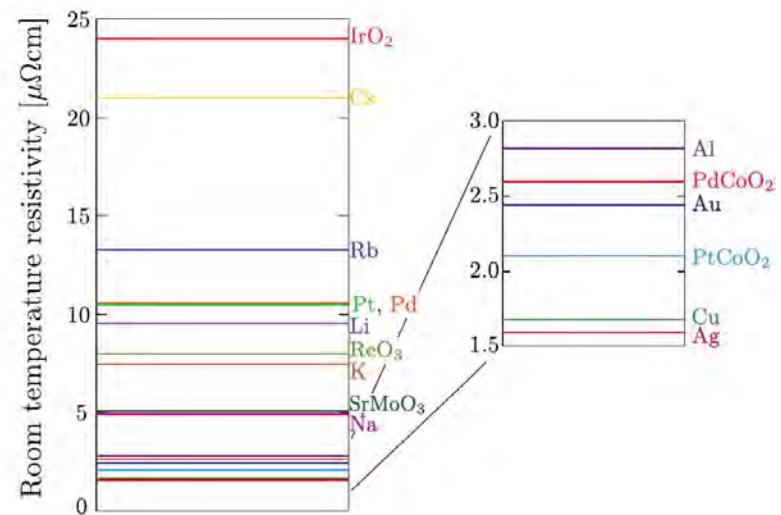
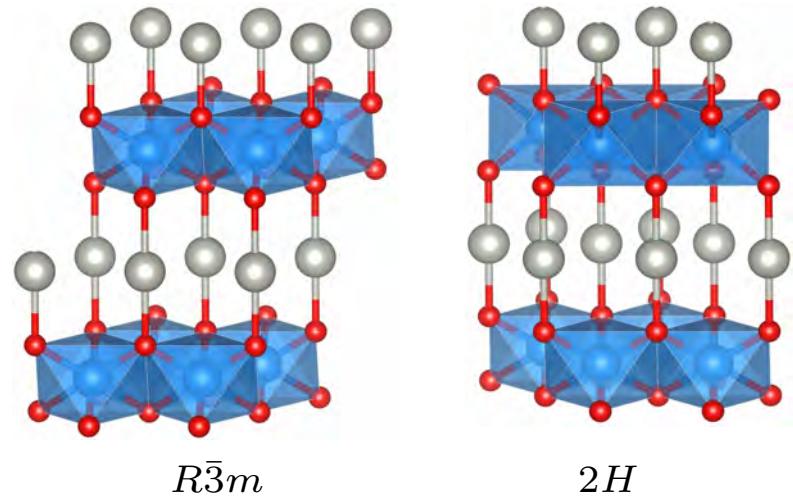
# Delafoossites: Introduction

[Mackenzie, Rep. Prog. Phys. 80, 032501 (2017)]

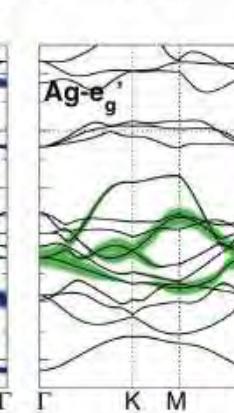
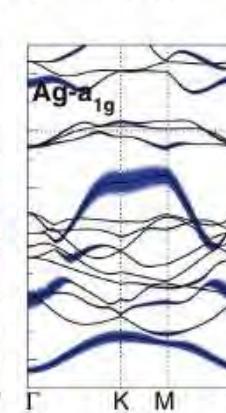
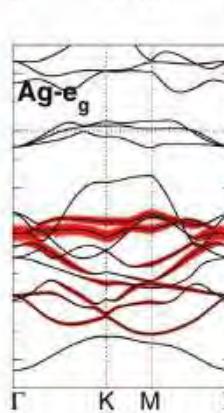
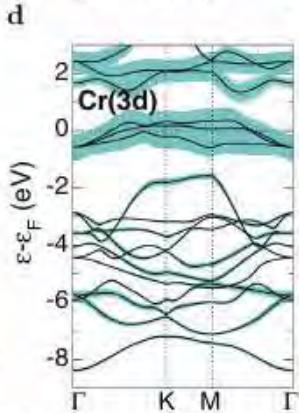
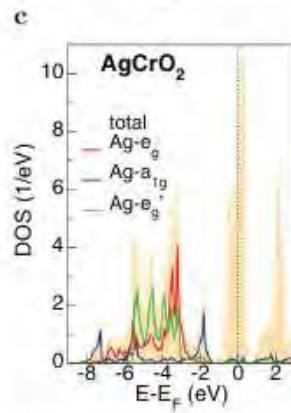
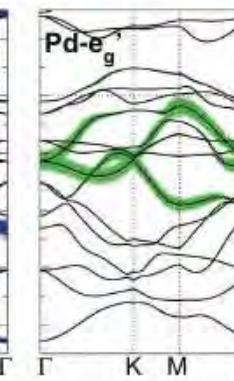
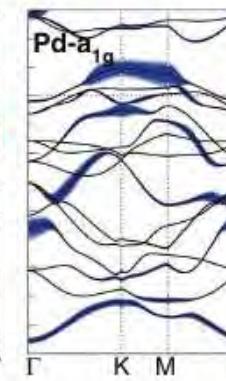
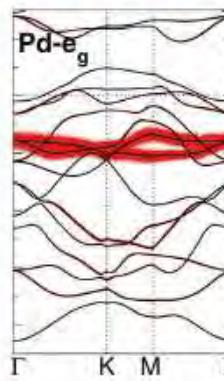
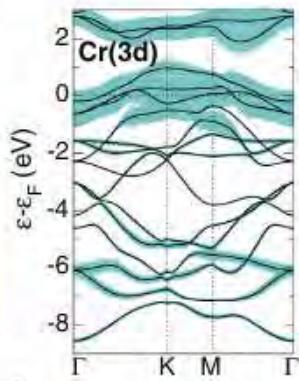
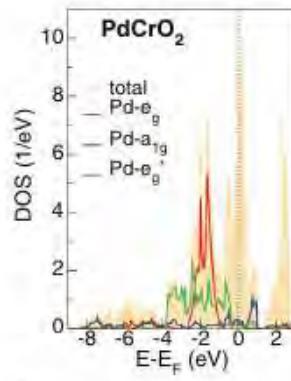
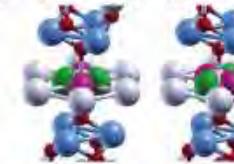
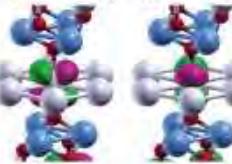
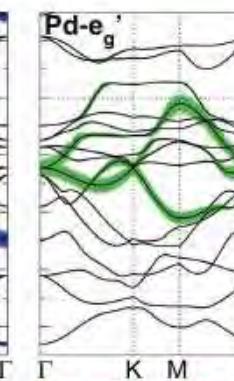
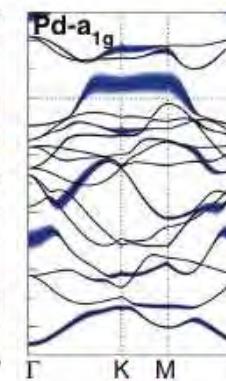
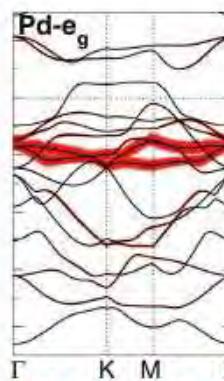
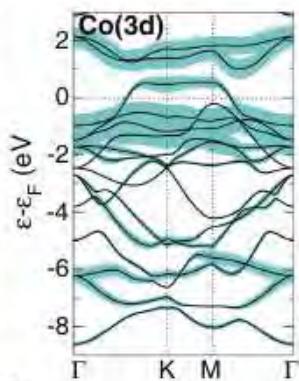
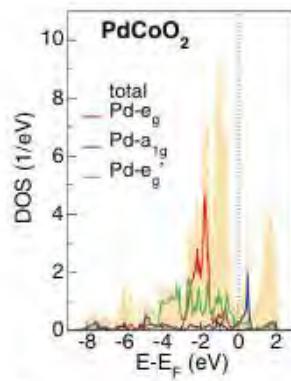
[FL, npj Comput Mater 7, 120 (2021)]

- natural oxide heterostructure  $\text{ABO}_2$ , with metallic  $\text{A}^+$  ions and metallic  $\text{B}^{3+}$  ions
- alternating A layers and  $\text{BO}_2$  layers
- A layer forms triangular lattice
- unique dumbbell O-A-O structure of connecting layers
- two stackings  
 $R\bar{3}m$ : e.g.  $\text{PdCoO}_2$ ,  $\text{CuCrO}_2$ , etc. (most)  
 $2H$ : e.g.  $\text{AgNiO}_2$
- wide variety of compounds, insulators and metals, with metals among highest conducting materials!

→ playground to design correlation physics

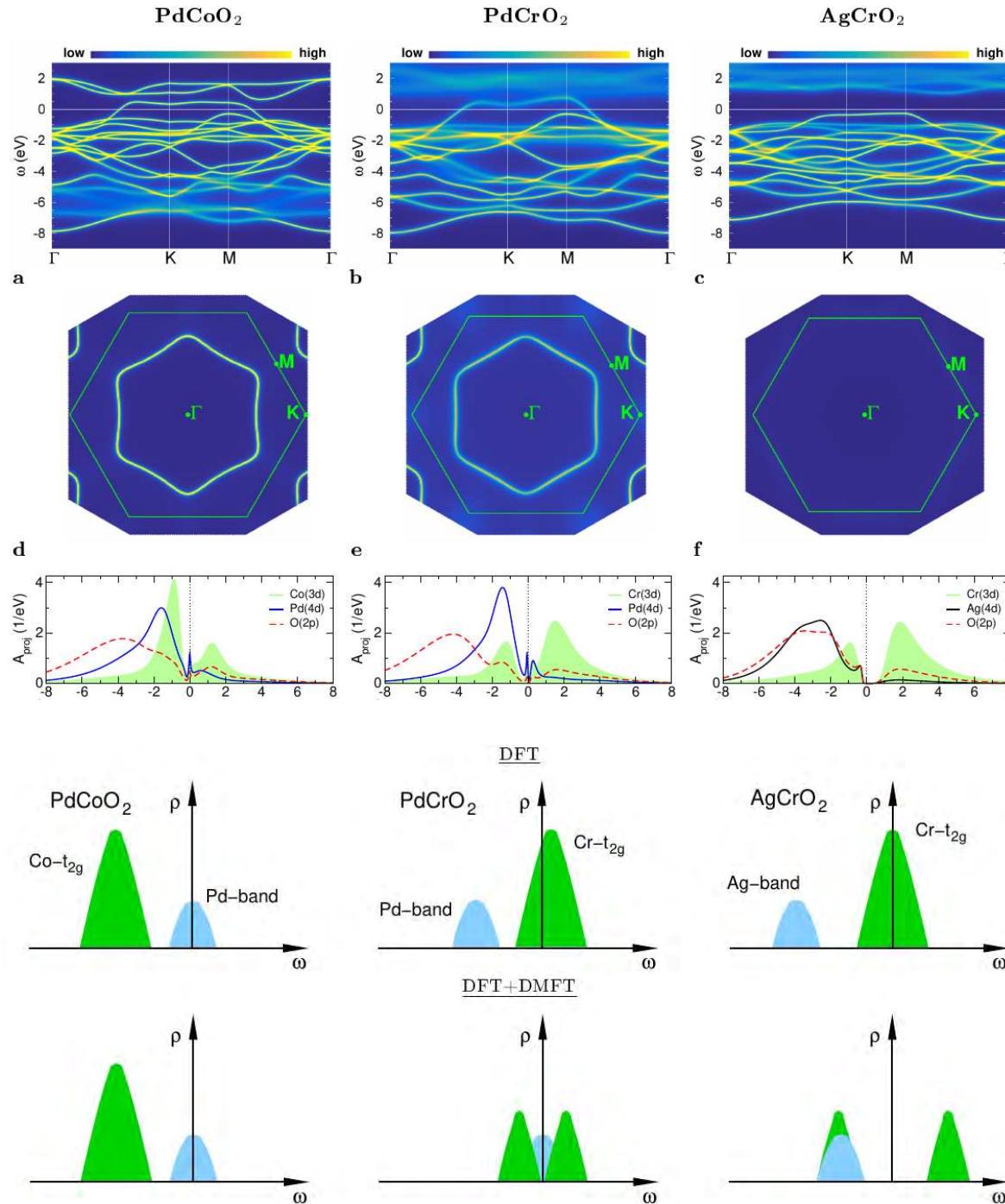


# Delafossites: DFT picture

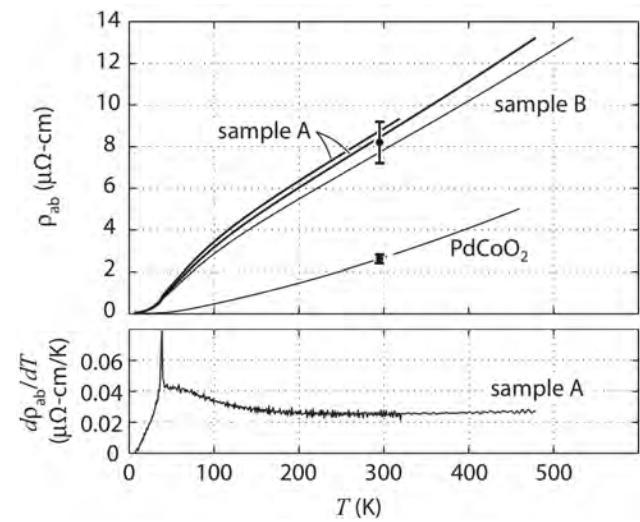


# Delafoossites: Correlation Scenarios

[FL, npj Comput Mater 7, 120 (2021)]



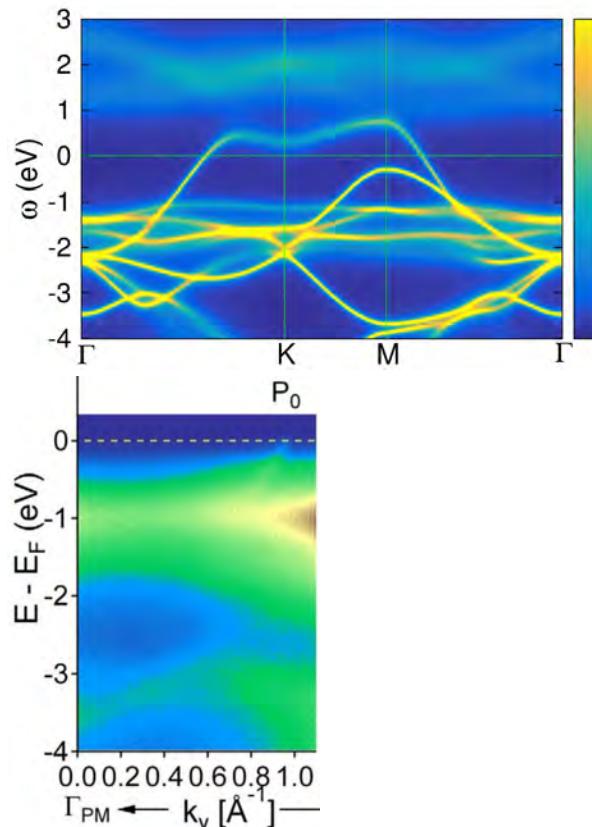
•  $U(\text{Co,Cr}) = 3 - 4 \text{ eV},$   
 $J_H = 0.7 \text{ eV}$



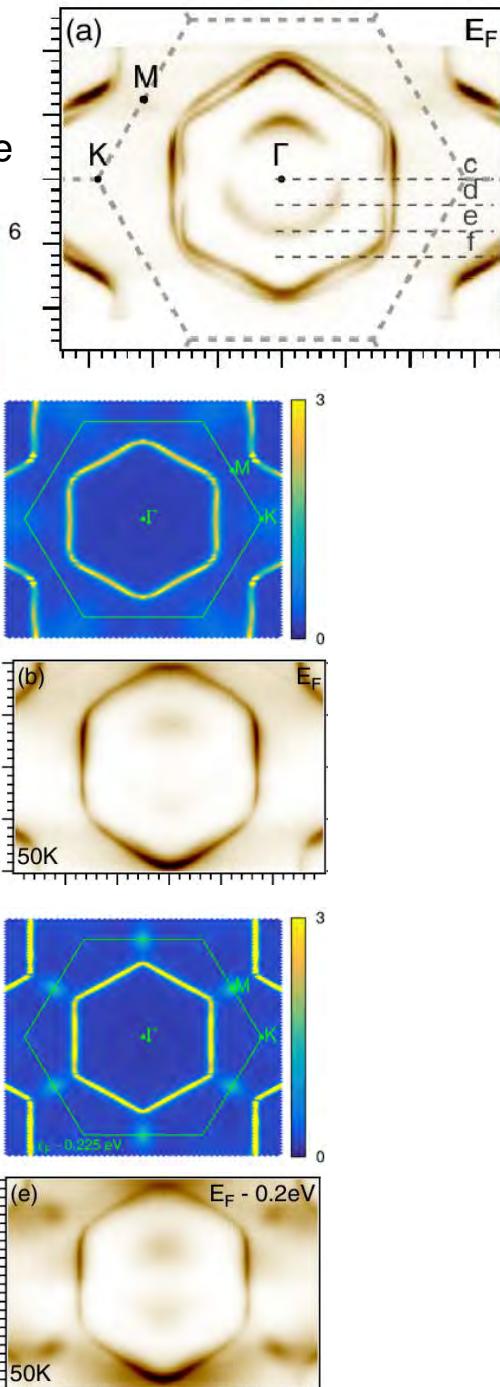
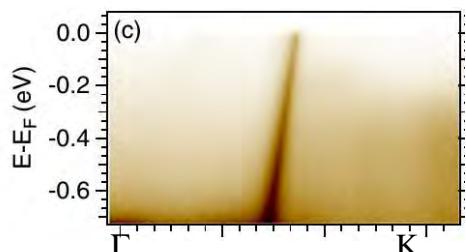
[Hicks et al, PRB 92, 014425 (2015)]

# Delafossites: PdCrO<sub>2</sub> Correlated Electronic Structure

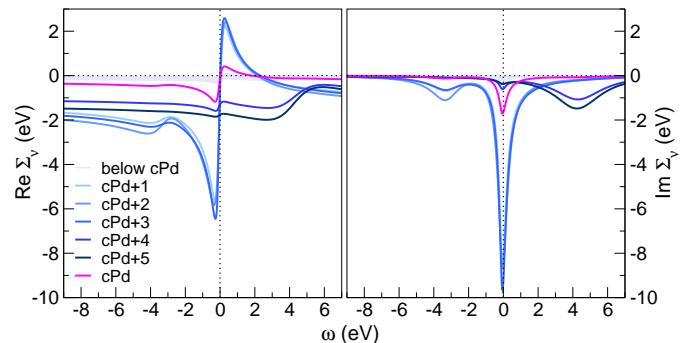
ARPES comparison in PM phase



100 K [Noh et al., Sci. Rep. 4, 3680 (2014)]



Coupling between itinerant and localized electrons



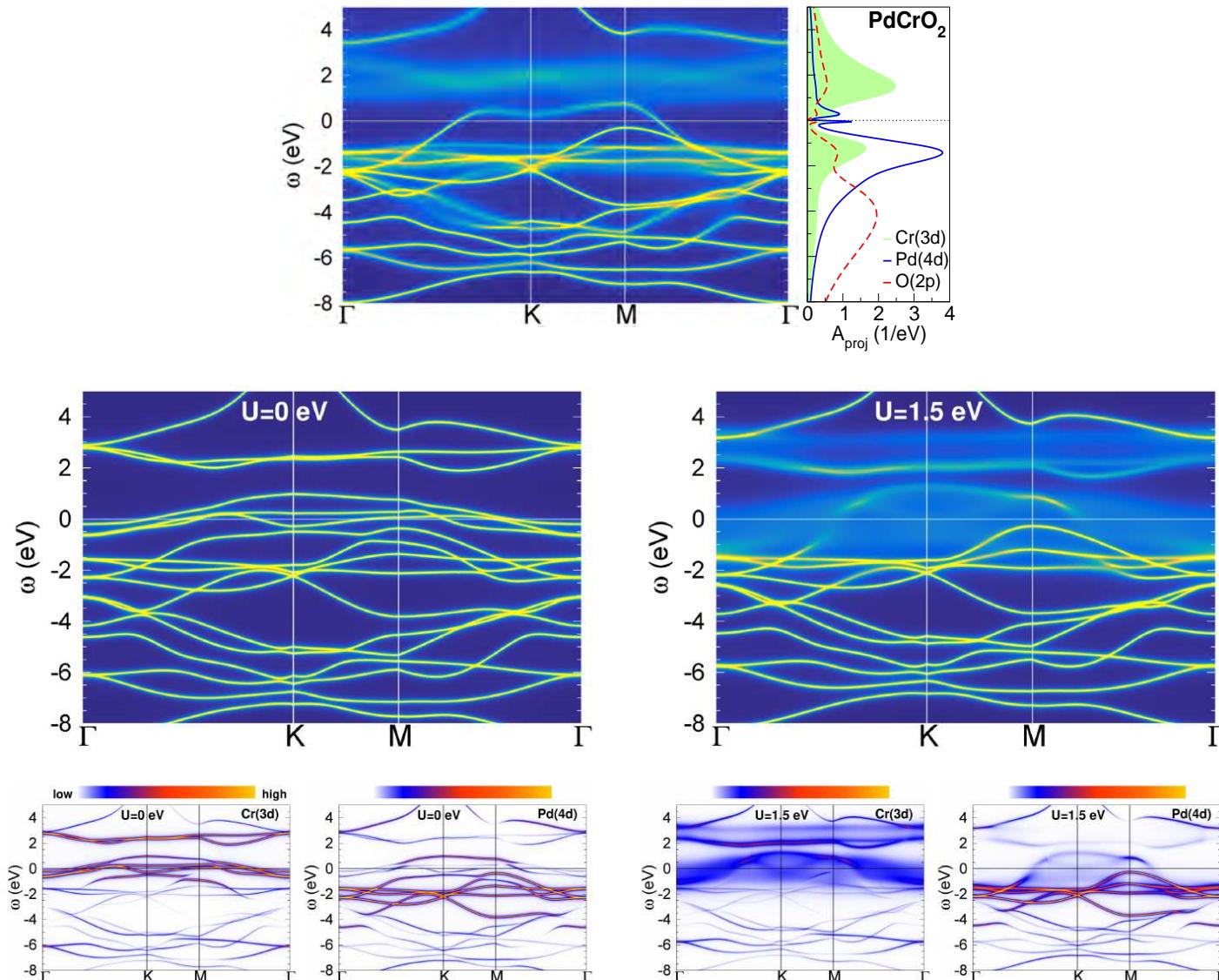
- from upfolded Cr self energy

$$\Sigma_{\nu\nu'}(\mathbf{k}, \omega) = \sum_{\mathbf{R}, m m'} \bar{P}_{\nu m}^{\mathbf{R}}(\mathbf{k}) \tilde{\Sigma}_{m m'}^{\mathbf{R}}(\omega) \bar{P}_{m' \nu'}^{\mathbf{R}}(\mathbf{k})$$

- significant self-energy contribution to conducting Pd band (no Hubbard interactions on Pd)
- relevant ee-scattering between Pd and CrO<sub>2</sub> layers
- Periodic Anderson model? Kondo model?

# Delafoossites: PdCrO<sub>2</sub> from weak to strong coupling

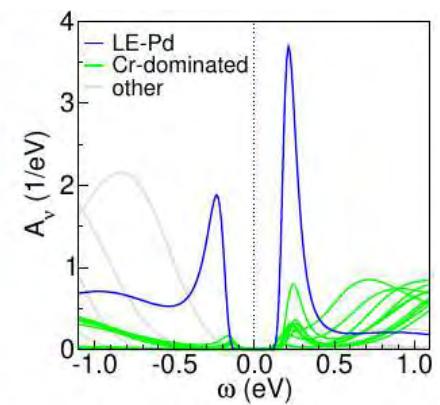
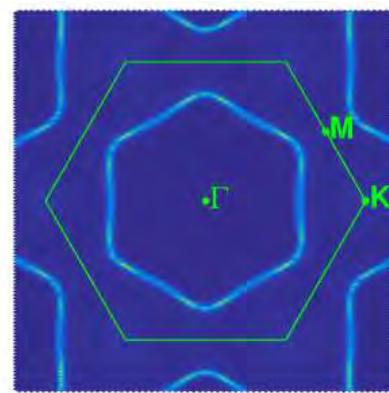
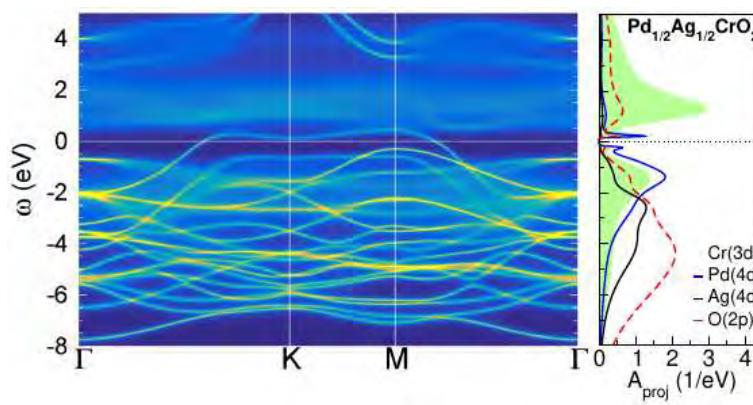
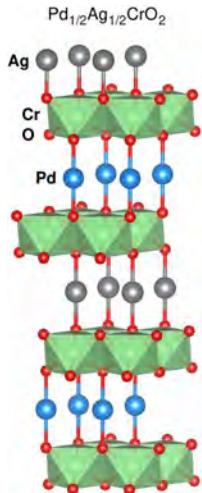
[FL, npj Comput Mater 7, 120 (2021)]



- metal-to-metal transition with growing interaction strength
- doping with isovalent Mo(4d) for Cr(3d)?

# Delafossites: PdCrO<sub>2</sub> Mott Design I

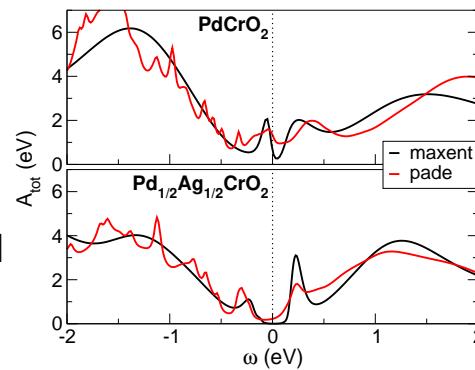
[FL, npj Comput Mater 7, 120 (2021)]



prediction

very weak dispersion crossing Fermi level

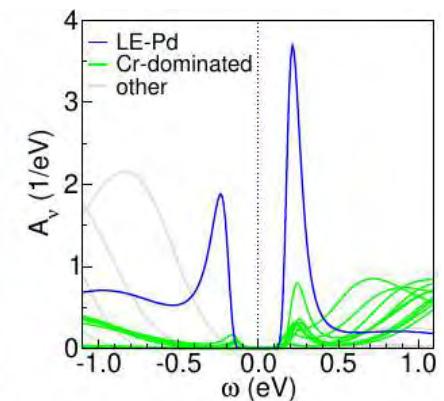
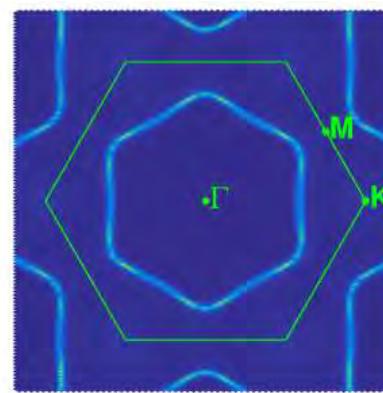
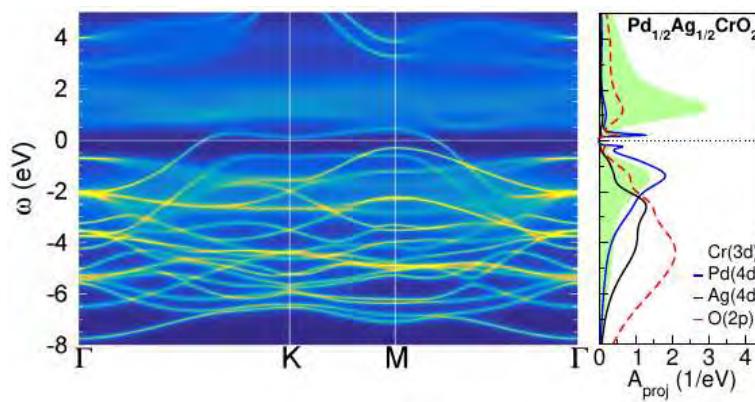
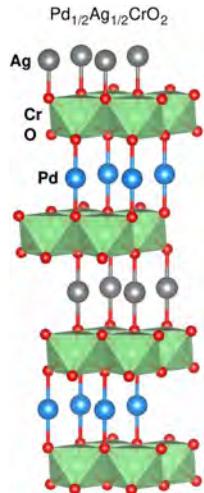
→ correlation-induced semimetal  
(CIS)



(no maxent artifact!)

# Delafossites: PdCrO<sub>2</sub> Mott Design I

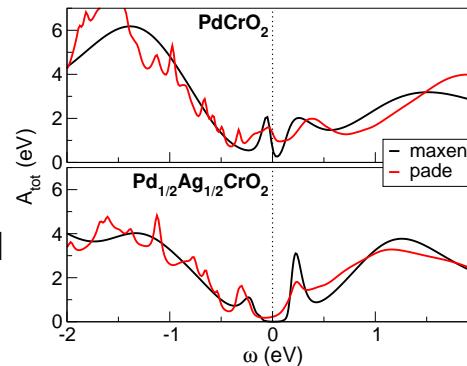
[FL, npj Comput Mater 7, 120 (2021)]



prediction

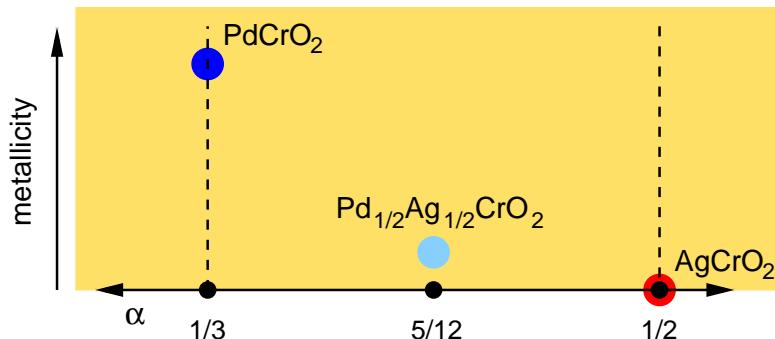
very weak dispersion crossing Fermi level

→ correlation-induced semimetal  
(CIS)



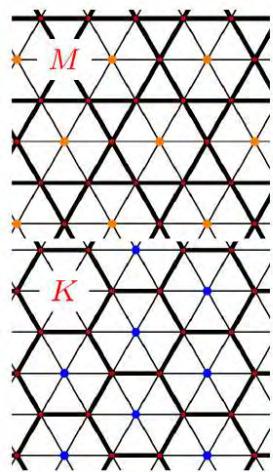
(no maxent artifact!)

strange metal inbetween hidden-Mott and Mott insulator

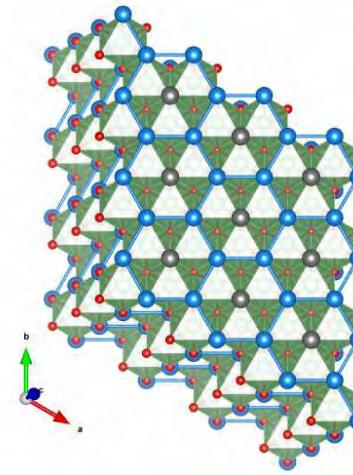
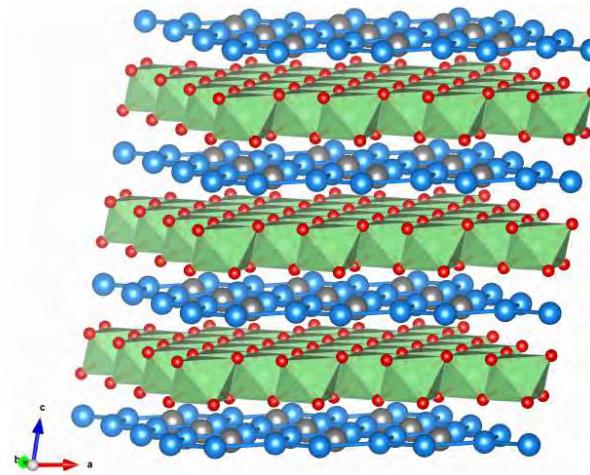


# Delafossites: $\text{PdCrO}_2$ Mott Design II

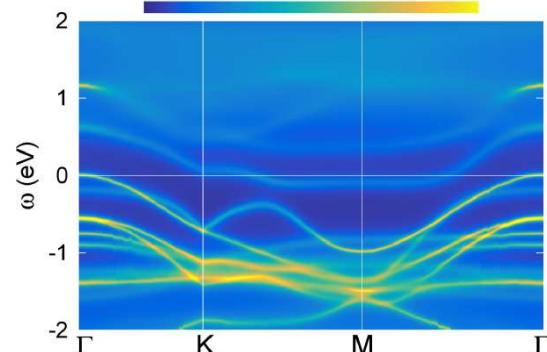
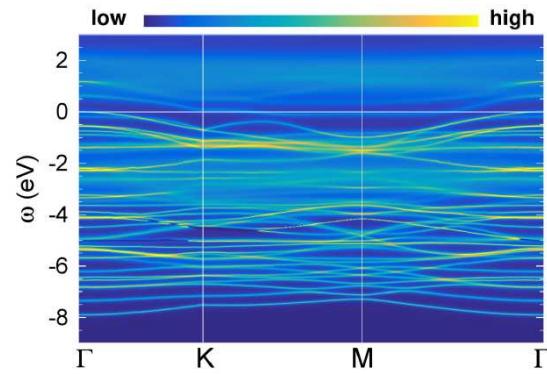
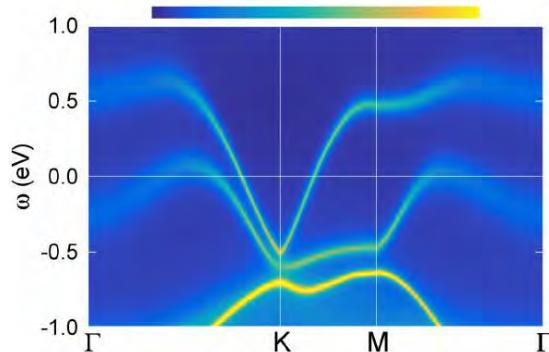
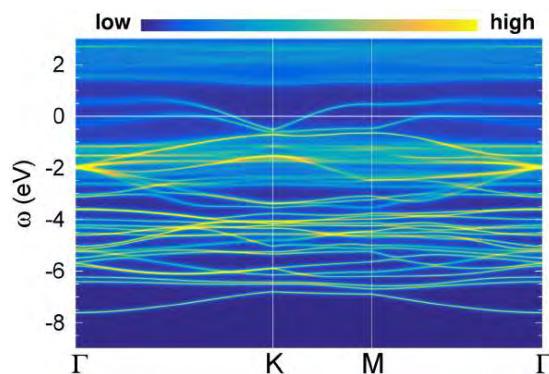
[FL, npj Comput Mater 7, 120 (2021)]



honeycomb-type (K)



kagomé-type (M)



# Summary

- DFT+Many-Body methodology is capable of addressing oxide-heterostructure challenges on a realistic level
- LaAlO<sub>3</sub>/SrTiO<sub>3</sub> interface
  - electronic correlations and defects are relevant to allow for intricate physics
  - 2DES vs. in-gap weight dichotomy
- $\delta$ -doping of titanate Mott insulators
  - layer-selective Mott transitions
  - triggering the AFM-to-FM criticality
- delafossites
  - natural heterostructures (“model system”)
  - various design options, to be further explored

Density Functional Theory (DFT) + Dynamical Mean-Field Theory (DMFT)

